

# DOCUMENT RESUME

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**IDENTIFIERS** Military Curriculum Project

## ABSTRACT

This individualized learning module on parallel circuits is one in a series of modules for a course in basic electricity and electronics. The course is one of a number of military-developed curriculum packages selected for adaptation to vocational instructional and curriculum development in a civilian setting. Four lessons are included in the module: (1) Rules for Voltage and Current, (2) Rules for Resistance and Power, (3) Variational Analysis, and (4) Troubleshooting Parallel Circuits. Each lesson follows a typical format including a lesson overview, a list of study resources, the lesson content, a programmed instruction section, and a lesson summary. (Progress checks are provided for each lesson in a separate document, CE 026 562.) (LRA)

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ED190883

NAVEDTRA 34258-6

CHIEF OF NAVAL EDUCATION AND TRAINING

MARCH 1977

# Military Curricula for Vocational & Technical Education

BASIC ELECTRICITY AND ELECTRONICS  
INDIVIDUALIZED LEARNING SYSTEM.

MODULE SIX. PARALLEL CIRCUITS.

STUDY BOOKLET.

U.S. DEPARTMENT OF HEALTH,  
EDUCATION & WELFARE  
NATIONAL INSTITUTE OF  
EDUCATION

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THE NATIONAL CENTER  
FOR RESEARCH IN VOCATIONAL EDUCATION  
THE OHIO STATE UNIVERSITY

### MILITARY CURRICULUM MATERIALS

The military-developed curriculum materials in this course package were selected by the National Center for Research in Vocational Education Military Curriculum Project for dissemination to the six regional Curriculum Coordination Centers and other instructional materials agencies. The purpose of disseminating these courses was to make curriculum materials developed by the military more accessible to vocational educators in the civilian setting.

The course materials were acquired, evaluated by project staff and practitioners in the field, and prepared for dissemination. Materials which were specific to the military were deleted, copyrighted materials were either omitted or approval for their use was obtained. These course packages contain curriculum resource materials which can be adapted to support vocational instruction and curriculum development.

## Military Curriculum Materials Dissemination Is . . .

an activity to increase the accessibility of military-developed curriculum materials to vocational and technical educators.

This project, funded by the U.S. Office of Education, includes the identification and acquisition of curriculum materials in print form from the Coast Guard, Air Force, Army, Marine Corps and Navy.

Access to military curriculum materials is provided through a "Joint Memorandum of Understanding" between the U.S. Office of Education and the Department of Defense.

The acquired materials are reviewed by staff and subject matter specialists, and courses deemed applicable to vocational and technical education are selected for dissemination.

The National Center for Research in Vocational Education is the U.S. Office of Education's designated representative to acquire the materials and conduct the project activities.

### Project Staff:

Wesley E. Budke, Ph.D., Director  
National Center Clearinghouse

Shirley A. Chase, Ph.D.  
Project Director

## What Materials Are Available?

One hundred twenty courses on microfiche (thirteen in paper form) and descriptions of each have been provided to the vocational Curriculum Coordination Centers and other instructional materials agencies for dissemination.

Course materials include programmed instruction, curriculum outlines, instructor guides, student workbooks and technical manuals.

The 120 courses represent the following sixteen vocational subject areas:

Agriculture	Food Service
Aviation	Health
Building & Construction	Heating & Air Conditioning
Trades	Machine Shop
Clerical	Management & Supervision
Occupations	Meteorology & Navigation
Communications	Photography
Drafting	Public Service
Electronics	
Engine Mechanics	

The number of courses and the subject areas represented will expand as additional materials with application to vocational and technical education are identified and selected for dissemination.

## How Can These Materials Be Obtained?

Contact the Curriculum Coordination Center in your region for information on obtaining materials (e.g., availability and cost). They will respond to your request directly or refer you to an instructional materials agency closer to you.

### CURRICULUM COORDINATION CENTERS

**EAST CENTRAL**  
Rebecca S. Douglass  
Director  
100 North First Street  
Springfield, IL 62777  
217/782-0759

**MIDWEST**  
Robert Patton  
Director  
1515 West Sixth Ave.  
Stillwater, OK 74704  
405/377-2000

**NORTHEAST**  
Joseph F. Kelly, Ph.D.  
Director  
225 West State Street  
Trenton, NJ 08625  
609/292-6562

**NORTHWEST**  
William Daniels  
Director  
Building 17  
Airdustrial Park  
Olympia, WA 98504  
206/753-0879

**SOUTHEAST**  
James F. Shill, Ph.D.  
Director  
Mississippi State University  
Drawer DX  
Mississippi State, MS 39762  
601/325-2510

**WESTERN**  
Lawrence F. H. Zane, Ph.D.  
Director  
1776 University Ave.  
Honolulu, HI 96822  
808/948-7834

## The National Center Mission Statement

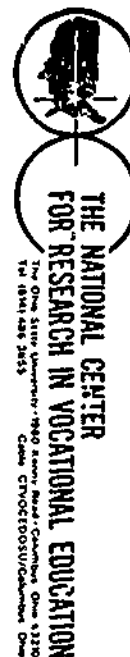
The National Center for Research in Vocational Education's mission is to increase the ability of diverse agencies, institutions, and organizations to solve educational problems relating to individual career planning, preparation, and progression. The National Center fulfills its mission by:

- Generating knowledge through research
- Developing educational programs and products
- Evaluating individual program needs and outcomes
- Installing educational programs and products
- Operating information systems and services
- Conducting leadership development and training programs

### FOR FURTHER INFORMATION ABOUT Military Curriculum Materials

#### WRITE OR CALL

Program Information Office  
The National Center for Research in Vocational  
Education  
The Ohio State University  
1960 Kenny Road, Columbus, Ohio 43210  
Telephone: 614/486-3655 or Toll Free 800/  
848-4815 within the continental U.S.  
(except Ohio)



## Military Curriculum Materials for Vocational and Technical Education

Information and Field  
Services Division

The National Center for Research  
in Vocational Education



## O V E R V I E W

### MODULE VI

#### PARALLEL CIRCUITS

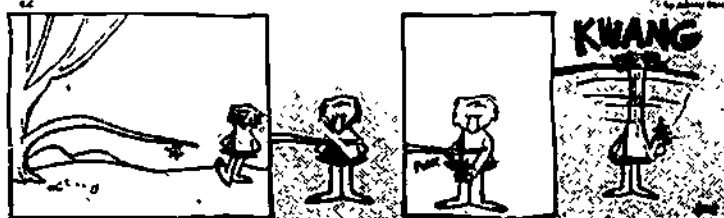
In this module you will learn the rules that govern the characteristics of parallel circuits; the relationships between voltage, current, resistance, and power; and the results of common troubles in parallel circuits.

For you to more easily learn the above, this module has been divided into the following four lessons:

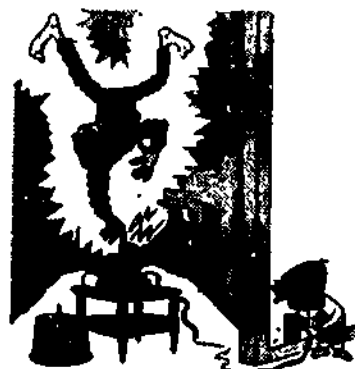
Lesson I.	Rules for Voltage and Current . . . . .
Lesson II.	Rules for Resistance and Power. . . . .
Lesson III.	Variational Analysis . . . . .
Lesson IV.	Troubleshooting Parallel Circuits . . . . .

TURN TO THE FOLLOWING PAGE AND BEGIN LESSON I.





If you don't know what it does don't fool with it!



**ACCIDENTS**  
don't just happen—  
**THEY ARE CAUSED!**

BASIC ELECTRICITY AND ELECTRONICS  
INDIVIDUALIZED LEARNING SYSTEM



MODULE VI  
LESSON I

Rules for Voltage and Current

Study Booklet



OVERVIEW

LESSON 4.

Rules for Voltage and Current

In this lesson you will study and learn about the following:

- how Ohm's Law is applied to parallel circuits
- voltage
- current
- practical solutions

Each of the above topics will be discussed in the order listed. As you proceed through this lesson, observe and follow directions carefully.

BEFORE YOU START THIS LESSON, PREVIEW THE LIST OF STUDY RESOURCES ON THE NEXT PAGE.

LIST OF STUDY RESOURCES  
LESSON 1

Rules for Voltage and Current

To learn the material in this lesson, you have the option of choosing, according to your experience and preferences, any or all of the following:

STUDY BOXES:

Lesson Narrative  
Programmed Instruction  
Lesson Summary

ENRICHMENT MATERIAL:

NAVPERS 93400A-1a "Basic Electricity, Direct Current."  
Fundamentals of Electronics. Bureau of Naval Personnel.  
Washington, D.C.: U.S. Government Printing Office, 1965.

AUDIO/VISUAL:

Sound/Slide Presentation "Measurement of I & E in a Parallel Circuit"

YOU MAY NOW STUDY ANY OR ALL OF THE RESOURCES LISTED ABOVE. YOU MAY  
TAKE THE PROGRESS CHECK AT ANY TIME.

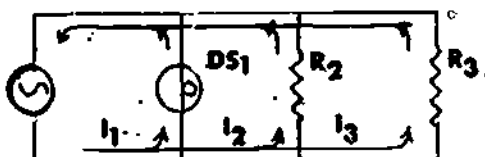
# NARRATIVE LESSON 1

## Rules for Voltage and Current

### A Look At Parallel Circuits

In the previous module you learned about Ohm's Law relationships and how they apply to series circuits. You learned certain rules about voltage, current, resistance, and power that are true for series circuits. It is now time to see how Ohm's Law is applied to parallel circuits.

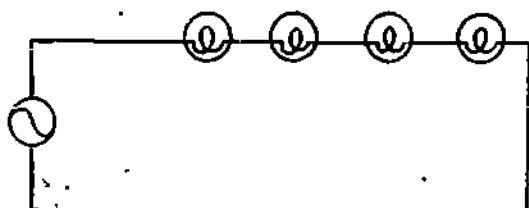
Recall that a parallel circuit is one which has more than one path for current to follow, although it has only one common source. Observing the schematic shown for a parallel circuit, you see one



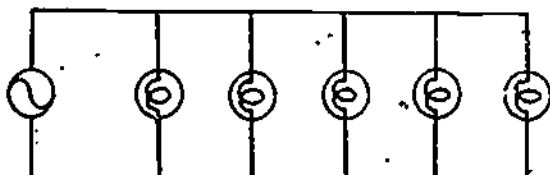
common source and three paths for current flow. Each path or branch supplies a load. Circuit configurations such as this are commonly used to wire homes and buildings.

Suppose that the parallel circuit illustrated above represents the wiring in your kitchen. Then DS1 might be the overhead light, R2 might be the toaster, and R3 the refrigerator. All three loads are fed by the same network of wires, from a common source.

Another wiring example you are probably familiar with is that of strings of Christmas tree lights. These strings may be wired either in series or in parallel as shown:



In series -- one path for current



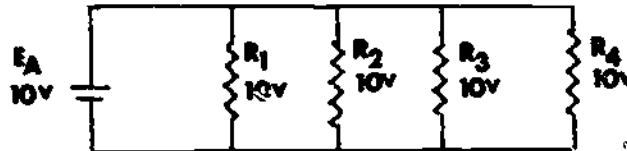
In parallel -- many paths for current

- You know that in the series string, if one lamp burns out, it opens the path so that no current can flow, and all of the lights go out.
- In the parallel string, this is not so. If one bulb in the parallel string burns out, it does not affect the other lights and they continue to glow. To see why this is so, we have to understand the relationships of current, voltage, and resistance in parallel circuits.

Voltage

You recall that in series circuits the same current flows through every component. This is not true of parallel circuits. In a Parallel network, voltage is common. That is, across each branch the voltage drop will equal the applied voltage. Because each branch is actually connected across the source, the same difference of potential will exist across each branch.

For example:



The applied voltage is 10v;  $E_{R1}$  is 10v;  $E_{R2}$  is 10v;  $E_{R3}$  is 10v; therefore, the voltage drop across  $R4$  will also be 10v. We can put this in a mathematical expression which reads:

$$E_{R1} = E_{R2} = E_{R3} = E_{R4} = E_a$$

The rule for voltage in series circuits (Kirchhoff's Voltage Law) is: "The sum of the voltage drops equals the applied voltage." In series circuits voltage is additive.

In parallel circuits, voltage is not additive. You do not add branch voltages in parallel circuits to solve for  $E_a$ . Applied voltage is the same as each branch voltage drop.

In this circuit, what is the value of:

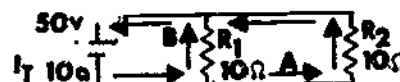


$E_{R1}$ ? \_\_\_\_\_  
 $E_{R3}$ ? \_\_\_\_\_  
 $E_a$ ? \_\_\_\_\_

Because the voltage is common across the elements of a parallel circuit, the voltage drops are all equal to each other, and the applied voltage is equal to any one of the individual voltage drops. In the circuit above,  $E_{R2}$  is 60v; therefore,  $E_{R1}$ ,  $E_{R3}$ , and  $E_a$  are also 60v.

Current

In a series circuit, the same current flows through every component. In a parallel circuit, the current in each branch is determined by the amount of resistance in the branch and the applied voltage.



In the circuit illustrated at the bottom of the previous page, with voltage 50v, total current is 10 amps as it leaves the source and arrives at junction A. Because each of the two branches has the same resistance, the 10 amps divides and 5 amps flows through the R1 branch, and 5 amps flows through the R2 branch. At junction B, the 5 amps from branch 2 joins the 5 amps from branch 1 to add up to a total current of 10 amps returning to the source.

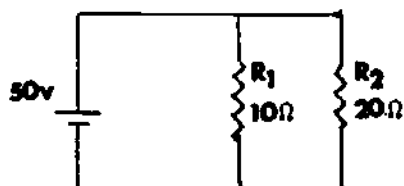
The following two rules apply to current in parallel circuits:

1. Each branch current is determined by the resistance of the branch.
2. Total current is equal to the sum of the branch currents.

Since electrons are neither created nor destroyed as the current divides, the sum of the currents flowing in the branches must be exactly equal to the total current flowing to and from the source.

### Solving for Branch Current

Ohm's Law is as true for parallel circuits as it is for series circuits. Therefore, by using the Ohm's Law formula  $I = \frac{E}{R}$ , you can determine the amount of current through a branch of a parallel network.



By Ohm's Law, determine the amount of current through R1 and R2.

$$I_{R1} = \underline{\hspace{2cm}}$$

$$I_{R2} = \underline{\hspace{2cm}}$$

Because voltage is common, if  $E$  is 50v, you know  $E_{R1}$  will be 50v and  $E_{R2}$  will be 50v. Applying Ohm's Law to find  $I$  through R1 (or  $I_{R1}$ ).

$$I_{R1} = \frac{E}{R1}$$

$$I_{R1} = \frac{50v}{10\Omega}$$

$$I_{R1} = 5a$$

To find  $I_{R2}$ :

$$I_{R2} = \frac{50v}{20\Omega}$$

$$I_{R2} = 2.5a$$

Solving for Total Current

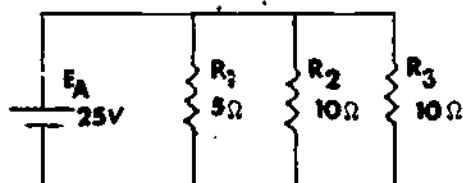
To find total  $I$  in a parallel circuit, we add the branch currents. Therefore, we can add  $I_{R1}$  and  $I_{R2}$  to find total current in the circuit we have been solving.

$$I_T = I_{R1} + I_{R2} + \dots + I_{Rn} \text{ (any number)}$$

$$I_T = 5a + 2.5a$$

$$I_T = 7.5a$$

The rule for parallel circuits that states the sum of the branch currents equals the total current is an application of what is referred to as Kirchhoff's Current Law; it is actually a statement of the law of conservation of matter, since at branch points, electrons are neither created nor destroyed.



Now solve this circuit.

$I_{R1}$	_____
$I_{R2}$	_____
$I_{R3}$	_____
$I_T$	_____

First you knew that voltage across each branch is equal to the applied voltage of 25v. By using Ohm's Law formula  $I = \frac{E}{R}$ , you should have determined that:

$$I_{R1} = 5a$$

$$I_{R2} = 2.5a$$

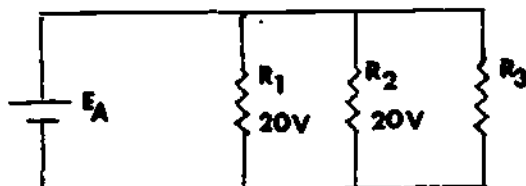
$$I_{R3} = 2.5a$$

Then, because the sum of branch currents equals total current,

$$I_T = 10a.$$

Practice

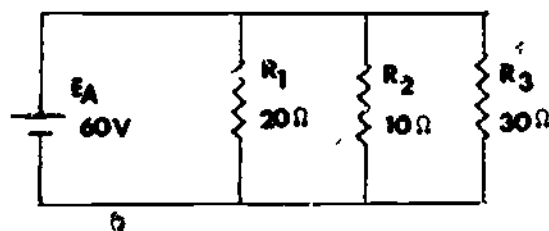
1. Solve for
- $E_{R3}$
- and
- $E_a$



$$E_{R3} = \underline{\hspace{2cm}}$$

$$E_a = \underline{\hspace{2cm}}$$

2. Solve for
- $I_1$
- ,
- $I_2$
- ,
- $I_3$
- and
- $I_T$
- (Note:
- $I_1$
- can be used just as
- $I_{R1}$
- , to indicate
- $I$
- through branch 1.)



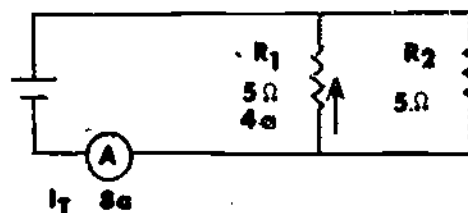
$$I_1 = \underline{\hspace{2cm}}$$

$$I_2 = \underline{\hspace{2cm}}$$

$$I_3 = \underline{\hspace{2cm}}$$

$$I_T = \underline{\hspace{2cm}}$$

3. Solve for
- $I_2$



$$I_2 = \underline{\hspace{2cm}}$$

Compare your answers with the correct answers on the next page.



## Answers to practice problems

1.  $E_{R3} = 20v$

$E_a = 20v$

Voltage is common. The voltage drop across each branch is equal to the applied voltage.

2.  $I_1 = 3a$

$I_2 = 6a$

$I_3 = 2a$

$I_T = 11a$

Since you know the values of  $E$  and  $R$ , you can apply Ohm's Law to find branch currents. The sum of the branch currents, then, equals the total current.

3.  $I_2 = 4a$

Since the sum of branch currents equals total current, you can subtract  $I_1$  from  $I_T$  to solve for  $I_2$ .

You could also have solved for voltage across  $R1$  ( $E = I \times R$ ).

Since  $E_{R1}$  is 20v,  $E_{R2}$  must also be 20v. Then by Ohm's Law you find:

$$I_{R2} = \frac{E_a}{R2}$$

$$I_{R2} = \frac{20v}{5\Omega}$$

$$I_{R2} = 4 \text{ amps}$$

AT THIS POINT, YOU MAY TAKE THE PROGRESS CHECK, OR YOU MAY STUDY ANY OF THE OTHER RESOURCES LISTED. IF YOU TAKE THE PROGRESS CHECK AND ANSWER ALL OF THE QUESTIONS CORRECTLY, GO TO THE NEXT LESSON. IF NOT, STUDY ANY METHOD OF INSTRUCTION YOU WISH UNTIL YOU CAN ANSWER ALL THE QUESTIONS CORRECTLY.

PROGRAMMED INSTRUCTION  
LESSON 1Rules for Voltage and Current

TEST FRAMES ARE 3, 7, 10, 13, 15 AND 25. GO FIRST TO TEST FRAME 3 AND SEE IF YOU CAN ANSWER ALL THE QUESTIONS THERE. FOLLOW THE DIRECTIONS GIVEN AFTER THE TEST FRAME.

---

1. As you recall, a series circuit has only one path for current flow. Because of this, the same current flows through all parts of the circuit. A parallel circuit, on the other hand, has more than one path or branch for current to flow through. As a result, the current divides and a different part of it flows in each of the branches.

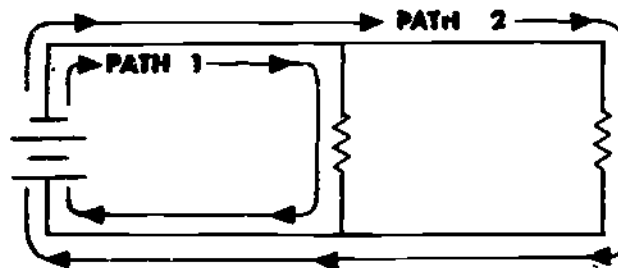
- a. A circuit with only one branch is a \_\_\_\_\_ circuit.  
b. A circuit with two or more paths is a \_\_\_\_\_ circuit.
- 

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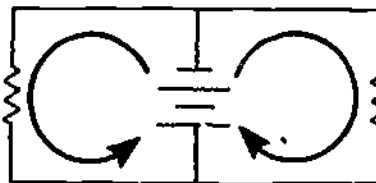
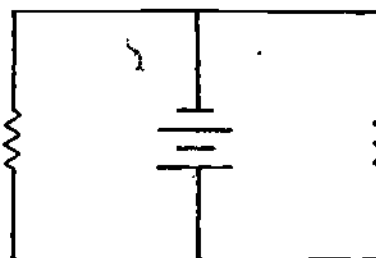
(a. series; b. parallel)

---

2. A parallel circuit has more than one circuit path connected to a common voltage source. A basic parallel circuit is represented in the schematic below, and the two current paths are shown by lines and arrowheads. Some electrons will take Path 1, and others will take Path 2.



Use lines and arrowheads to indicate the two current paths in this circuit:



3. Define a parallel circuit. \_\_\_\_\_
- \_\_\_\_\_
- \_\_\_\_\_

(THIS IS A TEST FRAME. COMPARE YOUR ANSWER WITH THE CORRECT ANSWER GIVEN AT THE TOP OF THE NEXT PAGE.)

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ANSWER - TEST FRAME 3

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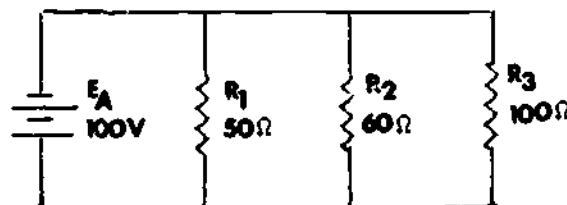
A parallel circuit is one which has more than one path for current flow connected to a common source.

---

IF YOUR ANSWER MATCHES THE CORRECT ANSWER, YOU MAY GO ON TO TEST FRAME 7. OTHERWISE, GO BACK TO FRAME 1 AND TAKE THE PROGRAMMED SEQUENCE BEFORE TAKING TEST FRAME 3 AGAIN.

---

4. Because there is only one path for current to flow in a series circuit, current is common. Current is not common in a parallel circuit because there is more than one path for current to flow. In a parallel circuit, the applied voltage is common. Look at the schematic below.



As you can see, both ends of each resistor are connected directly to the source, one side to the negative terminal, one to the positive terminal. This means that full source potential is impressed across each of the available current paths.

What value is common in parallel connections?

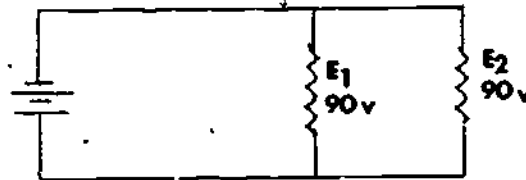
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(The applied voltage across each parallel component.)

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5. Source voltage in a parallel circuit is applied across each of the parallel loads. This can be easily seen, for there is almost no resistance between the source and either of the loads; therefore, there is almost no voltage drop between the source and each load.



The equation

$$E_s = E_1 = E_2 = \dots = E_n$$

states the above relationship, and indicates that voltage is the constant value in a parallel circuit.

What is the value of source voltage in this circuit?  $E_s =$  \_\_\_\_\_

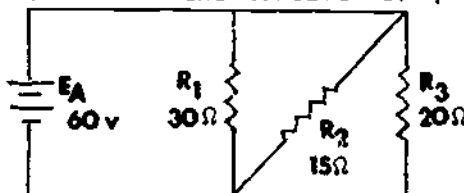
(90v - NOTE: At times  $E_s$ ,  $E_T$ ,  $E_a$ , or  $E_{bb}$  are used to indicate applied voltage.)

6. The resistance contained in the conductors of a circuit is so minute that for all practical purposes, it is neglected. Therefore, we can say that the voltage across each load in a parallel circuit is always \_\_\_\_\_ the applied voltage.

- \_\_\_\_\_ a. less than  
 \_\_\_\_\_ b. equal to  
 \_\_\_\_\_ c. greater than

(b) equal to

7. Solve the circuit for quantities indicated.



- a.  $E_{R2}$  \_\_\_\_\_  
 b.  $E_{R3}$  \_\_\_\_\_

(THIS IS A TEST FRAME. COMPARE YOUR ANSWERS WITH THE CORRECT ANSWERS GIVEN AT THE TOP OF THE NEXT PAGE.)

## ANSWERS - TEST FRAME 7

a. 60v

b. 60v

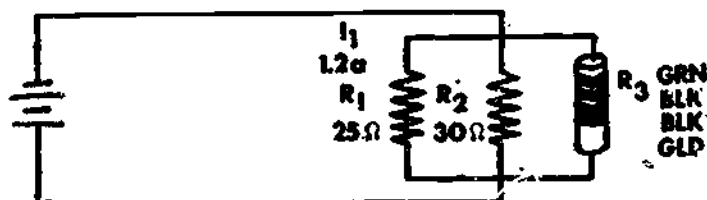
IF ALL YOUR ANSWERS MATCH THE CORRECT ANSWERS, YOU MAY GO ON TO TEST FRAME 10. OTHERWISE, GO BACK TO FRAME 4 AND TAKE THE PROGRAMMED SEQUENCE BEFORE TAKING TEST FRAME 7 AGAIN.

8. By now, you should have reached the conclusion that while \_\_\_\_\_ is common in a series circuit, \_\_\_\_\_ is common in a parallel circuit.

(current - voltage)

9. If the potential across any path is known or can be computed, source voltage is also known because voltage is the same in each branch of a parallel network.

What is the applied voltage?

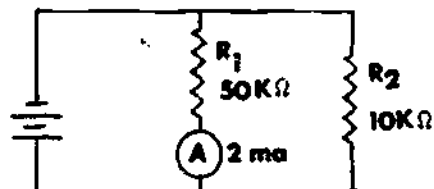


(30v)

P.1.

Six-1

10. Solve for  $E_a$ .



$E_a =$  \_\_\_\_\_

---

(THIS IS A TEST FRAME. COMPARE YOUR ANSWER WITH THE CORRECT ANSWER GIVEN AT THE TOP OF THE NEXT PAGE.)



---

 ANSWER - TEST FRAME 10
 

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100v

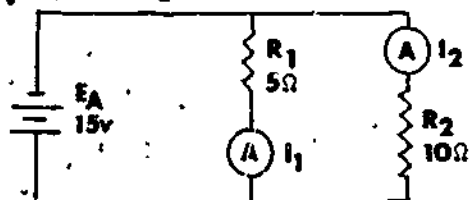
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IF YOUR ANSWER MATCHES THE CORRECT ANSWER, YOU MAY GO ON TO TEST FRAME 13. OTHERWISE, GO BACK TO FRAME 8 AND TAKE THE PROGRAMMED SEQUENCE BEFORE TAKING TEST FRAME 10 AGAIN.

---

11. Each of the current paths of a parallel circuit is called a branch. The current through each branch is independent of the current in the other branches, and is determined entirely by the source voltage and the resistance in the particular branch. Ohm's Law will provide the current value once the source voltage and the resistance of the branch are known ( $I = E/R$ ). Remember that current flow depends upon the voltage applied and the resistance opposing it. In a parallel circuit then, the current in each branch depends on the resistance of that branch.

Find  $I_1$  and  $I_2$  in the below circuit.



$I_1 =$  \_\_\_\_\_  
 $I_2 =$  \_\_\_\_\_

---

( $I_1 = 3a$ ;  $I_2 = 1.5a$ )

---

12. Branch currents are determined by the applied voltage, which is common to all branches of the circuit, and the \_\_\_\_\_ of the branch.
- 

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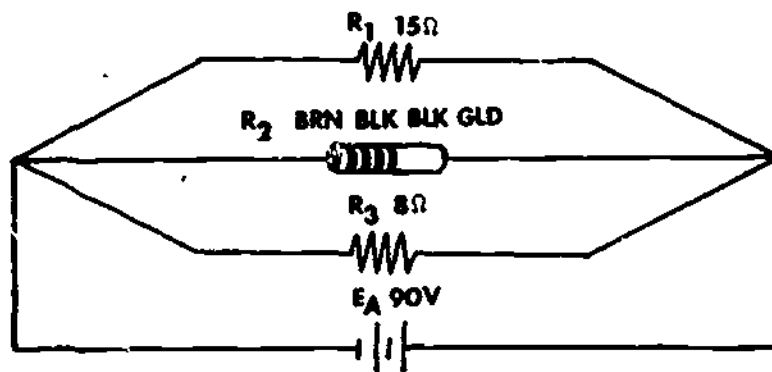
(resistance)

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P.1.

Six-1

13. Solve for  $I_{R2}$ .



$I_{R2} =$  \_\_\_\_\_

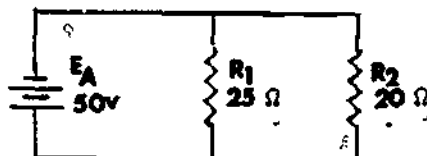
(THIS IS A TEST FRAME. COMPARE YOUR ANSWER WITH THE CORRECT ANSWER GIVEN AT THE TOP OF THE NEXT PAGE.)

## ANSWERS - TEST FRAME 13

9a

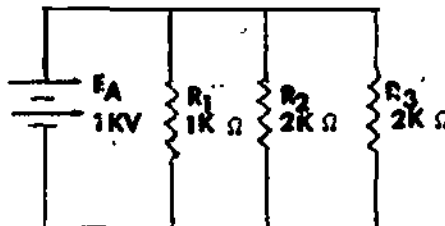
IF YOUR ANSWER MATCHES THE CORRECT ANSWER, YOU MAY GO ON TO TEST FRAME 15. OTHERWISE, GO BACK TO FRAME 11 AND TAKE THE PROGRAMMED SEQUENCE BEFORE TAKING TEST FRAME 13 AGAIN.

14. Total circuit current ( $I_T$ ) is equal to the sum of the individual branch currents. This is a statement of Kirchhoff's Current Law, expressed mathematically as  $I_T = I_1 + I_2 + I_3 + I_4$ , etc. (Since electrons are neither created nor destroyed, as the current divides, the sum of the currents in branches must exactly equal the total current.)

What is  $I_T$ ? $I_T =$  \_\_\_\_\_

( $I_T = 4.5a$ ;  $I_1 = 2a$ ;  $I_2 = 2.5a$ )

15. Solve for  $I_T$ .

 $I_T =$  \_\_\_\_\_

(THIS IS A TEST FRAME. COMPARE YOUR ANSWER WITH THE CORRECT ANSWER GIVEN AT THE TOP OF THE NEXT PAGE.)

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ANSWER - TEST FRAME 15

2a

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IF YOUR ANSWER MATCHES THE CORRECT ANSWER, YOU MAY GO ON TO TEST FRAME 25. OTHERWISE, GO BACK TO FRAME 14 AND TAKE THE PROGRAMMED SEQUENCE BEFORE TAKING TEST FRAME 15 AGAIN.

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16. As a review, perhaps a comparison between the two basic types of circuits would be helpful. As you are going through the problems that follow, note the similarities and differences between the two types of circuits.

The two basic types of circuits are \_\_\_\_\_.  
(Either order)

---



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(parallel and series)

---



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17. In a series circuit, current is the common value while the \_\_\_\_\_ divides among the various load devices.
- 
- 

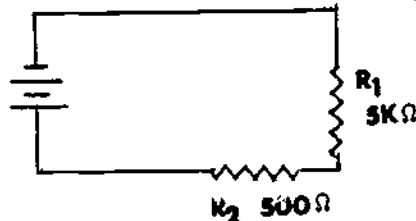
(voltage)

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18. Check the resistor that will have the greatest voltage drop.



\_\_\_ a. R1

\_\_\_ b. R2

---



---

(a) R1

---

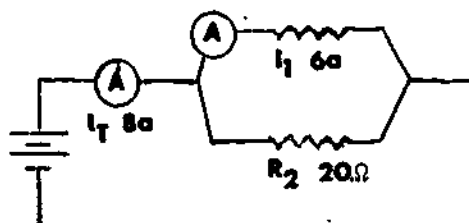


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19. In a parallel circuit, voltage is the common value while \_\_\_\_\_ divides among the branches.

(current)

20. Solve for  $E_a$ .



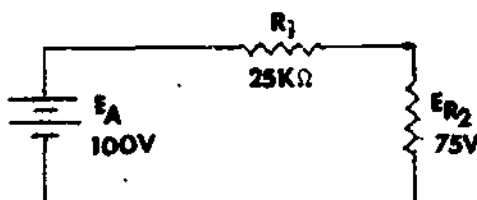
$E_a =$  \_\_\_\_\_

(40v)

21. In a series circuit,  $E_a = E_1 + E_2 + E_3$ , etc. This is a statement of \_\_\_\_\_.

(Kirchhoff's Voltage)

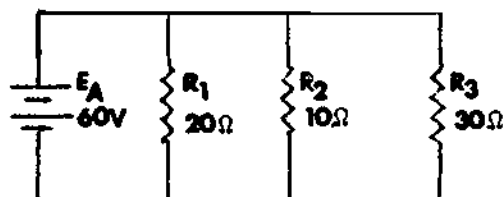
22. Solve for  $I_T$ .



$I_T =$  \_\_\_\_\_

(1ma)

23. Solve the circuit for quantities indicated.

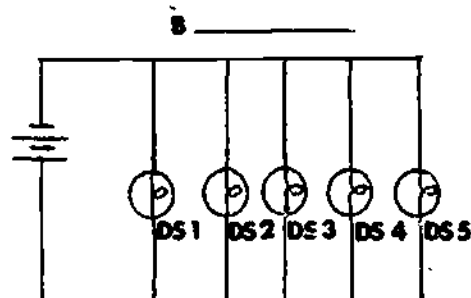
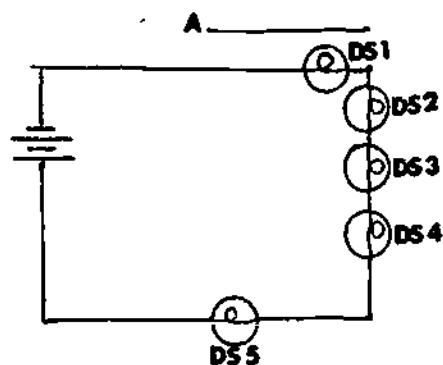


- a.  $I_1$  \_\_\_\_\_  
 b.  $I_2$  \_\_\_\_\_  
 c.  $I_3$  \_\_\_\_\_  
 d.  $I_T$  \_\_\_\_\_

(a. 3a; b. 6a; c. 2a; d. 11a)

24. One advantage of a parallel circuit over a series circuit becomes readily apparent when the two are compared.

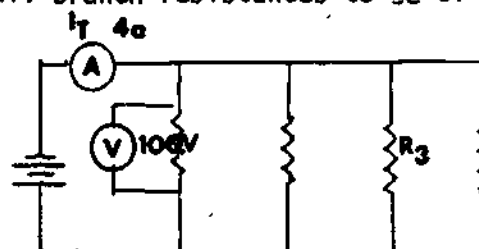
What would happen to lights DS2 through DS5 in each circuit, if DS1 were to burn out (filament opens)?



(A. All go out; B. DS2, DS3, DS4, DS5 remain lit)

25. Assume all branch resistances to be of equal value.

Solve:



$E_a$  \_\_\_\_\_

$R_3$  \_\_\_\_\_

(THIS IS A TEST FRAME. COMPARE YOUR ANSWERS WITH THE CORRECT ANSWERS GIVEN AT THE TOP OF THE NEXT PAGE.)

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ANSWERS - TEST FRAME 25

$$E_a = 100v$$

$$R_3 = 100\Omega$$

---

IF ANY OF YOUR ANSWERS ARE INCORRECT, GO BACK TO FRAME 16 AND TAKE THE PROGRAMMED SEQUENCE.

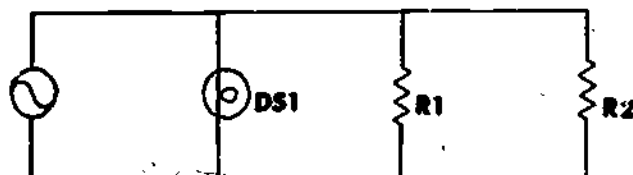
IF YOUR ANSWERS ARE CORRECT, YOU MAY TAKE THE PROGRESS CHECK, OR YOU MAY STUDY ANY OF THE OTHER RESOURCES LISTED. IF YOU TAKE THE PROGRESS CHECK AND ANSWER ALL THE QUESTIONS CORRECTLY, GO ON TO THE NEXT LESSON. IF NOT, STUDY ANY METHOD OF INSTRUCTION YOU WISH UNTIL YOU CAN ANSWER ALL THE QUESTIONS CORRECTLY.



# SUMMARY LESSON 1

## Rules for Voltage and Current

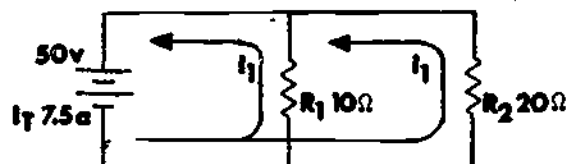
You have learned to apply several rules and laws to series circuits, and now it's time to apply similar rules and laws to parallel circuits. A parallel circuit, remember, is one which has more than one current path from a common source. The power outlets in your classroom, barracks, and home are all wired in parallel. Here is a schematic diagram for a parallel circuit with three current paths:



Christmas tree lights are available as either series or parallel strings. In the series string, one open lamp will cause all the lights to go off, but an open lamp in the parallel string will not affect any of the other lamps. This is so because current in a branch of a parallel circuit is independent of the current in any other branch; voltage is the quantity which is common. IN the schematic shown above, each component or branch is wired directly to the source, so the voltage applied to each component or branch is the same. Mathematically, the voltages would be written:  $E_a = E_1 = E_2 = E_3 = E_4$ , etc., where  $E_1$  is

the voltage applied across the first path for current flow (branch);  $E_2$ , the voltage across the second branch, etc. Remember that you add voltage drops in a series circuit, but all the voltages in the branches of a parallel circuit have the same value.

In contrast to current in a series circuit, current in a parallel circuit is not a common quantity everywhere in the circuit. Current in each branch depends on the resistance in that branch. This example may help you see this point.



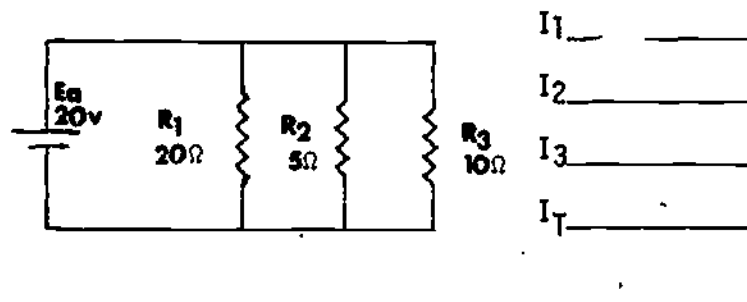
The 50 volts from the source is applied directly to  $R_1$  and to  $R_2$ , thus, according to Ohm's Law, the current through  $R_1$  is 5 amps and current through  $R_2$  is 2.5 amps. Since both currents are supplied by the battery, current flow to and from the battery is 7.5 amps, which is the sum of the branch currents. Mathematically, the current is:  $I_T = I_1 + I_2 + I_3$ , etc. You now have two rules for parallel circuits:

1. Voltage is the same across all branches of a parallel circuit ( $E_a = E_1 = E_2 = E_3$ , etc.)

2. Total current in a parallel circuit is equal to the sum of all branch currents. ( $I_T = I_1 + I_2 + I_3$ , etc.)

The second rule above is an application of Kirchhoff's Current Law, which is actually a statement of the law of conservation of matter. As an equation, we see  $I_T = I_1 + I_2 + I_3 + \dots + I_n$  where  $I_1$  is current in the first branch,  $I_2$  is current in the second branch, and  $I_n$  is the current through the last branch of whatever number of branches there are. Since electrons are neither created or destroyed as the current divides, the sum of the currents flowing in the branches must be exactly equal to the total current flowing to and from the source.

As a check, solve this problem for.



Answers -  $I_1 = 1a$ ;  $I_2 = 4a$ ;  $I_3 = 2a$ ;  $I_T = 7a$

AT THIS POINT, YOU MAY TAKE THE LESSON PROGRESS CHECK, OR YOU MAY STUDY THE LESSON NARRATIVE OR THE PROGRAMMED INSTRUCTION OR BOTH. IF YOU TAKE THE PROGRESS CHECK AND ANSWER ALL OF THE QUESTIONS CORRECTLY, GO TO THE NEXT LESSON. IF NOT, STUDY ANOTHER METHOD OF INSTRUCTION UNTIL YOU CAN ANSWER ALL THE QUESTIONS CORRECTLY.

BASIC ELECTRICITY AND ELECTRONICS  
INDIVIDUALIZED LEARNING SYSTEM



MODULE SIX  
LESSON II

Rules for Resistance and Power

Study Booklet

OVERVIEW  
LESSON II

Rules for Resistance and Power

In this lesson you will study and learn about the following:

- determining branch resistance
- equivalent resistance
- effect of adding resistors
- configurations
- methods of solution for equivalent resistance
- power
- practical application

Each of the above topics will be discussed in the order listed. As you proceed through this lesson, observe and follow directions carefully.

BEFORE YOU START THIS LESSON, PREVIEW THE LIST OF STUDY RESOURCES ON THE NEXT PAGE.

## LIST OF STUDY RESOURCES

## LESSON 11

Rules for Resistance and Power

To learn the material in this lesson, you have the option of choosing, according to your experience and preferences, any or all of the following:

## STUDY BOOKLET:

Lesson Narrative  
Programmed Instruction  
Lesson Summary

## ENRICHMENT MATERIAL:

NAVPERS 93400A-1a "Basic Electricity, Direct Current."  
Fundamentals of Electronics. Bureau of Naval Personnel.  
Washington, D.C.: U.S. Government Printing Office, 1965.

NAVPERS 93492-7 "Prep Text."  
Mathematics Series, Volume 2. Bureau of Naval Personnel.  
Washington, D.C.: U.S. Government Printing Office, 1965.

YOU MAY NOW STUDY ANY OR ALL OF THE RESOURCES LISTED ABOVE. YOU MAY  
TAKE THE PROGRESS CHECK AT ANY TIME.

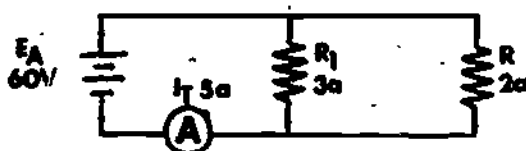
# NARRATIVE LESSON 11

## Rules for Resistance and Power

### Determining Branch Resistance

We have already discussed methods for solving for voltage and current in parallel circuits. Now we turn our attention to resistance.

When voltage and branch current are known, branch resistance can be determined by applying Ohm's Law. (Just as you did to solve for resistance in series circuits, you use the familiar formula,  $R = \frac{E}{I}$ .)



Find the values of:

R1. \_\_\_\_\_  
R2. \_\_\_\_\_

$$\text{Of course, } R1 = \frac{E}{I_{R1}}$$

$$R2 = \frac{E}{I_{R2}}$$

$$R1 = \frac{60v}{3a}$$

$$R2 = \frac{60v}{2a}$$

$$R1 = 20\Omega$$

$$R2 = 30\Omega$$

Now, using Ohm's Law, we can also determine the total or equivalent resistance of the circuit.

$$R_T = \frac{E}{I_T}$$

$$R = \frac{60v}{5a}$$

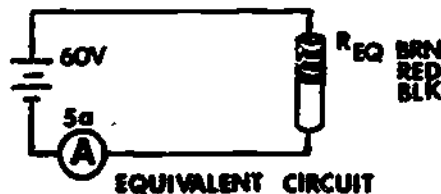
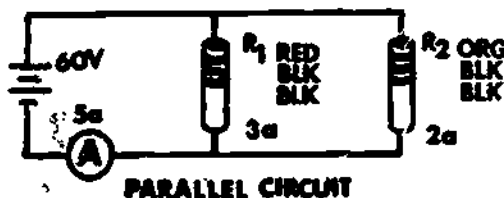
$$R = 12\Omega$$

Observe that although the parallel network had one resistor of 20  $\Omega$  (R1) and one of 30  $\Omega$  (R2), total circuit resistance is only 12  $\Omega$ .

A rule to remember here is that total resistance of a parallel network is always less than the smallest resistance of any branch.

### Equivalent Resistance or Total Resistance

When we lump the resistances of all branches of a parallel circuit into one imaginary resistor equal to the total resistance of the circuit, we call it the equivalent resistance or total resistance.



The total resistance of resistors in parallel is also referred to as EQUIVALENT RESISTANCE. In many texts the terms total resistance ( $R_T$ ) and equivalent resistance ( $R_{eq}$ ) are used interchangeably.

### Adding Resistors

Recall that in a series circuit, when we added a resistor, total resistance increased and total current decreased proportionately. Resistances are additive in series circuits.

Discover for yourself what happens when you add a branch resistance to a network.

You will need:

- multimeter set as ohmmeter.
- alligator clips for multimeter leads.
- two 10-ohm resistors.

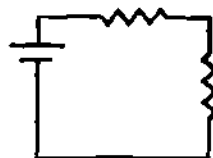
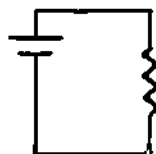
1. Clamp alligator clips of ohmmeter to both leads of one resistor.
2. Record approximate ohmmeter measurement. \_\_\_\_\_
3. Clamp the clips of ohmmeter to both leads of both resistors. (This adds a second resistor in parallel.)
4. Record approximate ohmmeter measurement. \_\_\_\_\_
5. When you add a branch resistor, what happens to total resistance? \_\_\_\_\_

Answer - When you added a resistor, the total network resistance decreased. This is true because you added another path for current, which increased the amount of total current with a corresponding decrease in the amount of total resistance.

1. If you change this series circuit:  
from \_\_\_\_\_ to \_\_\_\_\_

$R_T$  will

\_\_\_\_\_  
Increase/decrease



$I_T$  will

\_\_\_\_\_  
Increase/decrease



## Narrative

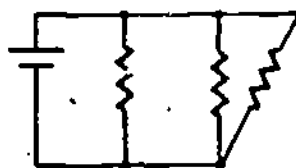
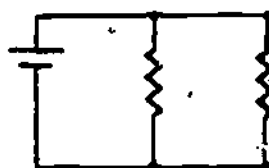
Six-11

2. If you change this parallel circuit:

$R_{eq}$  will

from

to



Increase/decrease

$I_T$  will

Increase/decrease

Answers: 1.  $R_T$  - increase

2.  $R_{eq}$  - decrease

$I_T$  - decrease

$I_T$  - increase

The rule to remember here is that adding a resistor to a parallel network decreases total resistance and provides a new path for current, and total current increases.

## A Word About Configurations

From now on some of the schematics we will work with will be unusual configurations. This is being done so you will become familiar with parallel networks as they might appear. You will seldom find parallel networks that look like neat boxes in real situations.

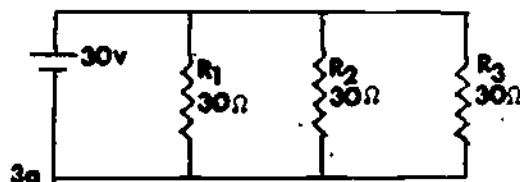
## Solving for Equivalent Resistance

To solve parallel circuits for total resistance or  $R_{eq}$ , there are several methods we can use. The selection of the method used depends on what information about the circuit is known.

### 1. Equal Branch Method

To find the  $R_{eq}$  when resistance is equal in each branch of the circuit, divide the ohmic value of one of the resistors by the number of branches.

$$R_{eq} = \frac{R}{n} \text{ (ohmic value of one resistance)} \\ \text{(number of branches)}$$



$$R_{eq} = \frac{30 \Omega}{3}$$

$$R_{eq} = 10 \Omega$$

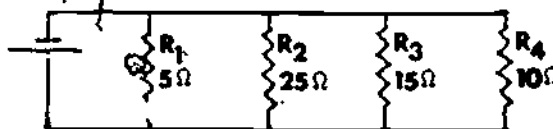
The following analysis of the equal branch method may help explain why the method works:

17. A very useful method of solving a parallel network of resistors for  $R_{eq}$  is called the assumed voltage method.

Any value of source voltage can be assigned (if none is given) and individual branch currents calculated (for the assumed voltage).

Adding all the branch currents gives  $I_T$ , and Ohm's Law can then be applied to get  $R_T$  ( $R_T = \frac{E_a}{I_T}$ ).

Example:



Any voltage can be assumed, but let's use 75v since the number 75 is divisible by all of the resistor values.

$$\text{Then, } I_1 = \frac{E_a}{R_1} = \frac{75v}{5\Omega} = 15a$$

$$I_2 = \frac{75v}{25\Omega} = 3a$$

$$I_3 = \frac{75v}{15\Omega} = 5a$$

$$I_4 = \frac{75v}{10\Omega} = 7.5a$$

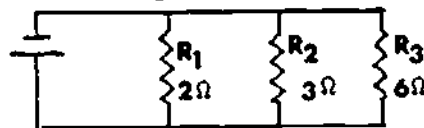
$$I_T = 30.5a$$

$$\text{and } R_T = \frac{E_a}{I_T} = \frac{75v}{30.5a} \approx 2.5\Omega \text{ (actually } 2.46\Omega)$$

( $\approx$  means approximately equal to.)

(NOTE: The only true value in this method is the value of resistance.)

Now, use the assumed voltage method to solve this network for  $R_T$ .



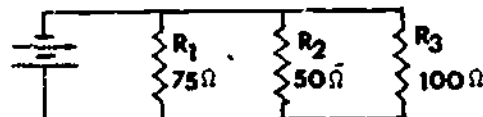
$R_T$  \_\_\_\_\_

---


$$(R_T = 1\Omega)$$


---

18. In the following circuit, no applied voltage is given and the resistance values are not equal.



One possible way of solving this problem is called the reciprocal method. This method can be used with any number of branches and  
(CONTINUED ON NEXT PAGE)

any values of resistance. The formula is a variation of the assumed voltage method and is derived from a combination of Kirchhoff's Current Law and Ohm's Law.

$$\frac{E_a}{R_T} = \frac{E_a}{R_1} + \frac{E_a}{R_2} + \frac{E_a}{R_3} \text{ etc.}$$

dividing both sides  
of the equations by  
 $E_a$  yields

$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \text{ etc.}$$

dividing both sides  
into 1 yields

$$R_T = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \dots \text{etc.}}$$

Now you can see that all you are really doing is assuming a voltage of 1v.

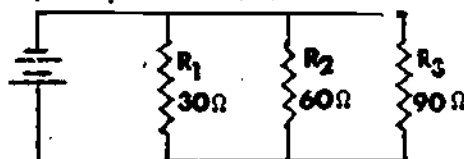
To solve, substitute values in formula:

$$R_{eq} = \frac{1}{\frac{1}{75} + \frac{1}{50} + \frac{1}{100}}$$

To combine the fractions, find the lowest common denominator. The most convenient way to do this is to pick the largest denominator and use it as the common denominator. Then determine how many times each of the denominators will go into this number and use these figures as the numerators:

$$R = \frac{1}{\frac{1.3}{100} + \frac{2}{100} + \frac{1}{100}} = \frac{1}{\frac{4.3}{100}} = \frac{100}{4.3} = 23.3 \Omega$$

Instead of dividing the fraction  $\frac{4.3}{100}$  into 1 as the formula implies, simply invert the fraction to  $\frac{100}{4.3}$  and divide 4.3 into 100. Mathematically, both procedures are the same.



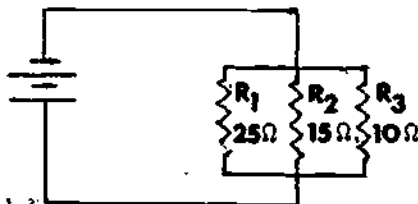
Find  $R_{eq}$  \_\_\_\_\_  $\Omega$

(16.36  $\Omega$ )

P.1:

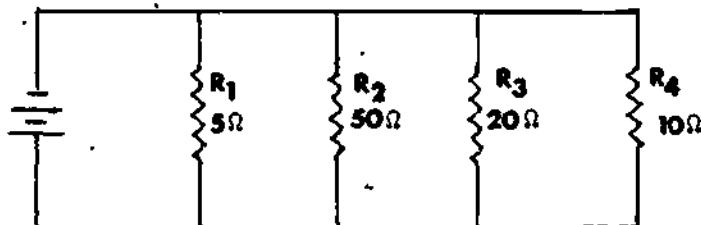
Six-11

19. Using the reciprocal method, solve for  $R_{eq}$ . \_\_\_\_\_  $\Omega$



(4.84  $\Omega$ )

20. Solve for  $R_{eq}$ . \_\_\_\_\_  $\Omega$



(THIS IS A TEST FRAME. COMPARE YOUR ANSWER WITH THE CORRECT ANSWER GIVEN AT THE TOP OF THE NEXT PAGE.)

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 ANSWER - TEST FRAME 20

 2.7Ω
 

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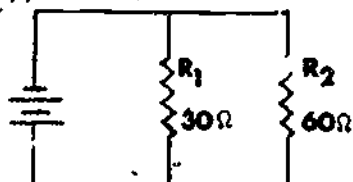
 IF YOUR ANSWER MATCHES THE CORRECT ANSWER, YOU MAY GO ON TO TEST FRAME 25. OTHERWISE, GO BACK TO FRAME 15 AND TAKE THE PROGRAMMED SEQUENCE BEFORE TAKING TEST FRAME 20 AGAIN.
 

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21. A somewhat simplified method of computing equivalent resistance is available, but can only be used with two branches at a time. The method is called product over the sum, represented mathematically as:

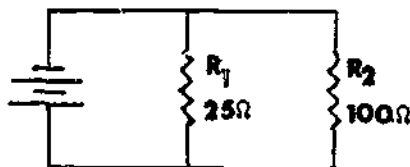
$$R_{eq} = \frac{R_1 \times R_2}{R_1 + R_2}$$

This formula can be applied to a circuit using the steps shown below:



1. Substitute values in formula  $R_{eq} = \frac{30 \times 60}{30 + 60}$
  2. Combine terms  $R_{eq} = \frac{1800}{90}$
  3. Final computation  $R_{eq} = 20 \Omega$
- 

What is  $R_{eq}$  \_\_\_\_\_ Ω




---

 (20 Ω)
 

---

22. Recall that in a series circuit total resistance could be determined simply by adding all the resistance values in the circuit.

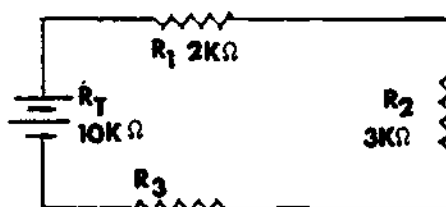
$$R_T = R_1 + R_2 + R_3$$

Adding another resistor in series would:

- ☐ a. decrease total resistance.  
☐ b. increase total resistance.

(b) increase total resistance

23. Solve for  $R_3$ . \_\_\_\_\_  $\Omega$



(5 kΩ)

24. In parallel circuits total current is always greater than current in any branch. Consequently, total parallel resistance is always smaller than any branch resistance.

Adding another resistor in parallel would:

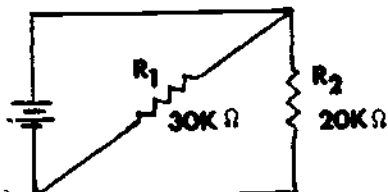
- ☐ a. increase total resistance.  
☐ b. decrease total resistance.

(b) decrease total resistance

P.1.

Six-11

25. Solve for  $R_{eq}$ . \_\_\_\_\_  $\Omega$



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(THIS IS A TEST FRAME. COMPARE YOUR ANSWER WITH THE CORRECT ANSWER GIVEN AT THE TOP OF THE NEXT PAGE.)

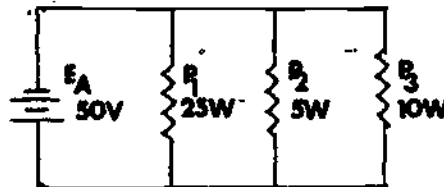
## ANSWERS - TEST FRAME 25

12 k $\Omega$ 

IF YOUR ANSWER MATCHES THE CORRECT ANSWER, YOU MAY GO ON TO TEST FRAME 28. OTHERWISE, GO BACK TO FRAME 21 AND TAKE THE PROGRAMMED SEQUENCE BEFORE TAKING TEST FRAME 25 AGAIN.

26. Power computations in a parallel circuit are the same as those used for series circuits. Since power dissipation in resistors consists of a heat loss, power dissipations are additive regardless of how the resistors are connected in the circuit.

Find  $P_T$ . \_\_\_\_\_ W

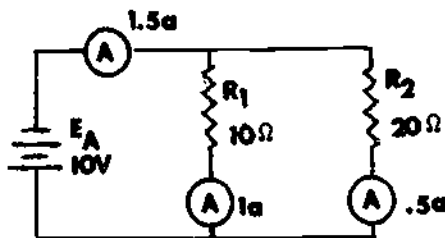


(40w)



27. The equations  $P = I^2 R$ ,  $P = \frac{E^2}{R}$ , and  $P = IE$  apply to any resistor or circuit so long as the values used are correct for that resistor or circuit. In other words, if you are looking for the power dissipated by a particular resistor use only the values associated with that resistor.

For example, in this circuit the amount of power dissipated by  $R_1$



will be 10 watts whether you use  $\frac{E^2}{R}$ ,  $P_I = E I_{R_1}$ ,  $P_{R_1} = I_{R_1}^2 R_1$ , or  $P_{R_1} = \frac{E^2}{R_1}$  to find the answer, but you will not get the correct answer if you use  $I_T$  or  $I_{R_2}$  or even  $R_2$  in your calculation. By the same token, total power may be found if  $I_T$ ,  $R_T$  and  $E$  (any  $E$ , since all are the same in parallel) are used.

Find  $P_T$  and  $P_{R_2}$  in the above circuit.  $P_T$  \_\_\_\_\_.  $P_{R_2}$  \_\_\_\_\_

( $P_T = 15w$ ,  $P_{R_2} = 5w$  NOTE: Because there will generally be more

than one valid method of solving any given problem and you will occasionally be using decimal numbers instead of whole numbers, the answers shown here will not always correspond exactly to the ones you compute.)

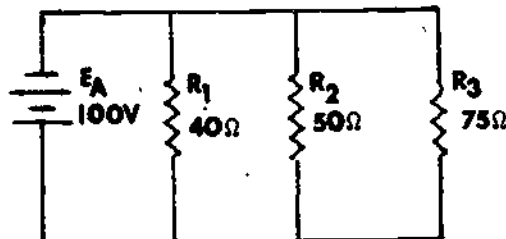
28. Solve for:

a.  $P_T$  \_\_\_\_\_

b.  $P_{R_1}$  \_\_\_\_\_

c.  $P_{R_2}$  \_\_\_\_\_

d.  $P_{R_3}$  \_\_\_\_\_



(THIS IS A TEST FRAME. COMPARE YOUR ANSWERS WITH THE CORRECT ANSWERS GIVEN AT THE TOP OF THE NEXT PAGE.)

## ANSWERS - TEST FRAME 28

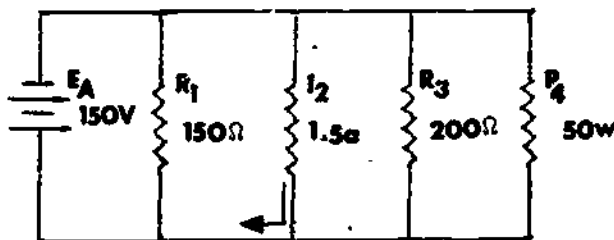
- a. 583w
- b. 250w
- c. 200w
- d. 133w

IF ALL YOUR ANSWERS MATCH THE CORRECT ANSWERS, YOU MAY GO ON TO TEST FRAME 32. OTHERWISE, GO BACK TO FRAME 26 AND TAKE THE PROGRAMMED SEQUENCE BEFORE TAKING TEST FRAME 28 AGAIN.

29. If two values from the same part of the circuit are known or can be computed, all of the other values for that part can be found. For example, if  $E$  and  $I$  are known, all of the total values can be computed; if  $P_{R2}$  and  $E_{R2}$  are known, all values for  $R2$  can be found.

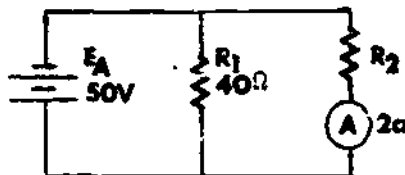
Solve for:

- a.  $I_{R4}$  \_\_\_\_\_
- b.  $P_{R3}$  \_\_\_\_\_
- c.  $R2$  \_\_\_\_\_
- d.  $P_{R1}$  \_\_\_\_\_



(a. 333ma or .33a; b. 112.5w; c.  $100\Omega$ ; d. 150w)

30. Solve for  $R_2$ . \_\_\_\_\_



(25  $\Omega$ )

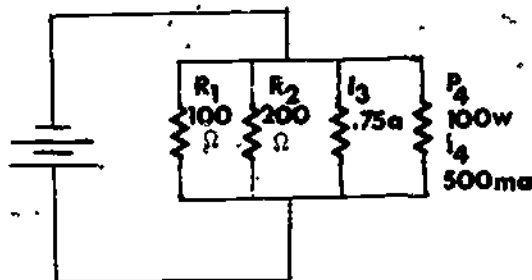
31. Keep in mind that if you want to find a value at one particular part of a circuit, you must know or be able to compute two other values at that point.

Solve for:

a.  $E_T$ . \_\_\_\_\_

b.  $I_T$ . \_\_\_\_\_

c.  $R_T$ . \_\_\_\_\_

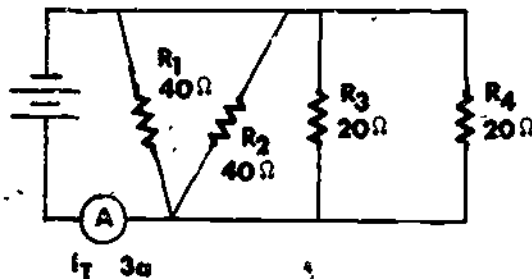


(a. 200v; b. 4.25a; c. 47 $\Omega$ )

32. Solve for:

a.  $P_{R2}$ . \_\_\_\_\_

b.  $P_T$ . \_\_\_\_\_



(THIS IS A TEST FRAME. COMPARE YOUR ANSWERS WITH THE CORRECT ANSWERS GIVEN AT THE TOP OF THE NEXT PAGE.)

## ANSWERS - TEST FRAME 32

a. 10w

b. 60w

IF ALL YOUR ANSWERS MATCH THE CORRECT ANSWERS, YOU MAY GO ON TO TEST FRAME 34. OTHERWISE, GO BACK TO FRAME 29 AND TAKE THE PROGRAMMED SEQUENCE BEFORE TAKING TEST FRAME 32 AGAIN.

33. As you will recall, resistors are rated in watts as well as ohms. The wattage rating of a resistor refers to its \_\_\_\_\_ heat dissipating capability.

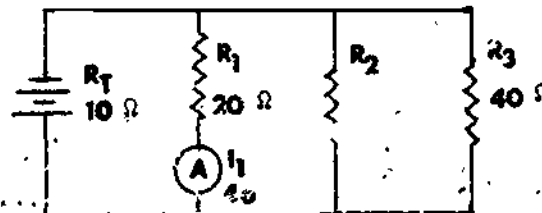
(maximum)

34. Check the resistor or resistors that would overheat.

\_\_\_ a. R1

\_\_\_ b. R2

\_\_\_ c. R3



All resistors are rated at 250w.

(THIS IS A TEST FRAME. COMPARE YOUR ANSWERS WITH THE CORRECT ANSWERS GIVEN AT THE TOP OF THE NEXT PAGE.)

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ANSWER - TEST FRAME 34

a. R1

---

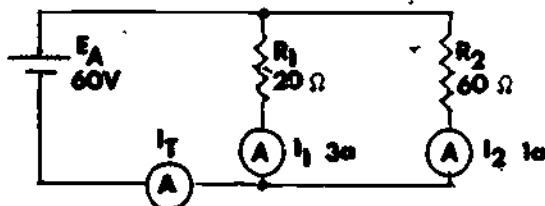
IF YOUR ANSWER IS INCORRECT, GO BACK TO FRAME 33 AND TAKE THE PROGRAMMED SEQUENCE.

IF YOUR ANSWER IS CORRECT, YOU MAY TAKE THE PROGRESS CHECK, OR YOU MAY STUDY ANY OF THE OTHER RESOURCES LISTED. IF YOU TAKE THE PROGRESS CHECK AND ANSWER ALL THE QUESTIONS CORRECTLY, GO ON TO THE NEXT LESSON. IF NOT, STUDY ANY METHOD OF INSTRUCTION YOU WISH UNTIL YOU CAN ANSWER ALL THE QUESTIONS CORRECTLY.

# SUMMARY LESSON 11

## Rules for Resistance and Power

In the following parallel circuit, the total resistance can be found by the form of Ohm's Law  $R_T = \frac{E}{I_T}$ , just as in a series circuit. When you calculate the total resistance in this circuit, you find that  $R_T$  is only 15 ohms -- less than the value of either  $R_1$  or  $R_2$ .

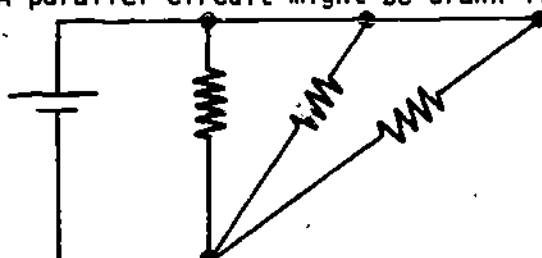


This rule holds true for any parallel circuit: The total resistance of a parallel circuit is always less than the smallest resistance of any of its branches.

A look at the above circuit will show why this is true. If the circuit contained only  $R_1$ , the total resistance would be 20 ohms and total current 3 amperes. Adding  $R_2$  in parallel creates a second current path, and total current from the source increases. So as far as the source is concerned, the resistance it sees is reduced, or  $R_T$  has become smaller.

The total resistance of resistors in parallel is also referred to as EQUIVALENT RESISTANCE. In many texts the terms total resistance and equivalent resistances are used interchangeably.

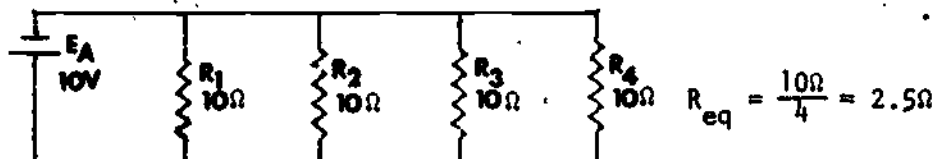
So far, all the schematic diagrams you have seen were drawn in nice, neat straight lines or boxes, but some of the schematics you will be seeing from now on may be drawn in a less orderly manner and not so easily understood. If you find one you do not readily understand, redraw it so that it makes sense to you while keeping all the same connections. A parallel circuit might be drawn like this:



You will obtain even stranger configurations while drawing a diagram from an actual circuit. In actual trouble-shooting techniques you will find, by re-drawing a circuit it will help simplify it for ease in locating the problem.

You have seen how to solve parallel circuits for  $R_T$  by finding total current, then using Ohm's Law to find  $R_T$ ; now you will see some methods

which are faster to use. For example, when all the branches of a network are equal in resistance, you can find  $R_{eq}$  by dividing the value of one of the resistors by the number of branches.



A parallel circuit with two unequal branches may be solved by the product over the sum method. The equation for this method is

$R_{eq} = \frac{R_1 \times R_2}{R_1 + R_2}$ , and all you need to do is insert the values and compute to get the equivalent resistance.

A method which you can use to solve a circuit with any number of branches is the reciprocal of the sum of the reciprocals method, or

$$R_{eq} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots + \frac{1}{R_n}}$$

Here is an example of how to use this equation:

$$\begin{aligned} R_{eq} &= \frac{1}{\frac{1}{10\Omega} + \frac{1}{15\Omega} + \frac{1}{30\Omega}} \\ &= \frac{1}{\frac{3}{30} + \frac{2}{30} + \frac{1}{30}} \\ &= \frac{1}{\frac{6}{30}} \\ &= \frac{30}{6} \\ &= 5\Omega \end{aligned}$$

This is a method which you can always depend on to give the equivalent resistance. Be sure to learn it.

Now let's move on to a study of power in parallel circuits. This should be an easy subject, for power in parallel circuits is found in exactly the same way as power in series circuits. Power in the branches can be found by either  $P = EI$  or  $P = I^2R$  or  $P = \frac{E^2}{R}$ , where the branch current, resistance and/or voltage is used in each case. (Remember,  $E$  or voltage difference was actually work per unit charge; since  $I$  is charge per second, the product of  $E$  and  $I$  is work per second, or power.) Total power is equal to  $EI_T$ ; it can also be found by adding the power dissipated in each branch ( $P_T = P_1 + P_2 + P_3 + \dots + P_n$ ). You may also use either total current or total voltage and equivalent

## Summary

Six-11

resistance in  $P_T = I_T^2 \times R_{eq}$  or  $P_T = \frac{E_T^2}{R}$ . You can prove any of these by making your own parallel circuit and working out the values by all these methods. All of your answers should agree.

AT THIS POINT, YOU MAY TAKE THE LESSON PROGRESS CHECK, OR YOU MAY STUDY THE LESSON NARRATIVE OR THE PROGRAMMED INSTRUCTION OR BOTH. IF YOU TAKE THE PROGRESS CHECK AND ANSWER ALL OF THE QUESTIONS CORRECTLY, GO TO THE NEXT LESSON. IF NOT, STUDY ANOTHER METHOD OF INSTRUCTION UNTIL YOU CAN ANSWER ALL THE QUESTIONS CORRECTLY.





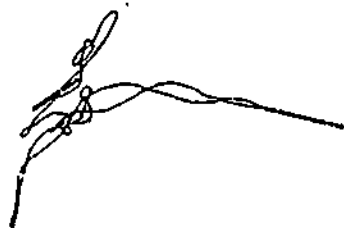
BASIC ELECTRICITY AND ELECTRONICS  
INDIVIDUALIZED LEARNING SYSTEM



MODULE SIX  
LESSON 111

Variational Analysis

Study Booklet



OVERVIEW  
LESSON III

Variational Analysis

In this lesson you will study and learn about the following:

- variable quantities
- changing voltage
- adding or removing a parallel resistor
- changing resistance in an existing branch

BEFORE YOU START THIS LESSON, PREVIEW THE LIST OF STUDY RESOURCES ON THE NEXT PAGE.

LIST OF STUDY RESOURCES  
LESSON III

Variational Analysis

To learn the material in this lesson, you have the option of choosing, according to your experience and preferences, any or all of the following:

STUDY BOOKLET:

- Lesson Narrative
- Programmed Instruction
- Lesson Summary

ENRICHMENT MATERIAL:

NAVPERS 93400A-1a "Basic Electricity, Direct Current."  
Fundamentals of Electronics. Bureau of Naval Personnel.  
Washington, D.C.: U.S. Government Printing Office, 1965.

YOU MAY NOW STUDY ANY OR ALL OF THE RESOURCES LISTED ABOVE. YOU MAY  
TAKE THE PROGRESS CHECK AT ANY TIME.

# NARRATIVE LESSON III

## Variational Analysis

In the past two lessons, you have learned the rules that apply to DC parallel circuits. Now we are going to look at the interrelationships between quantities in parallel networks to see what will happen to everything in the circuit if one quantity is changed. To conduct this variational analysis, we will use a simple table as shown.

$I_T$	
$R_T$	
$P_T$	
$I_{R1}$	
$I_{R2}$	
$I_{R3}$	
$E_{R1}$	
$E_{R2}$	
$E_{R3}$	
$R_1$	
$R_2$	
$R_3$	

In each empty box, we will indicate with an arrow whether a quantity will increase (+), decrease (-), or remain the same (→).

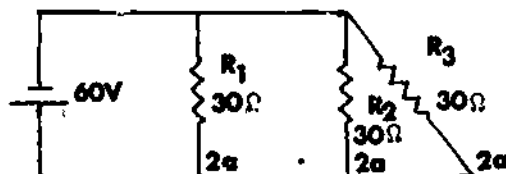
## Variable Quantities

There are three quantities that we can vary by increasing or decreasing:

1. the applied voltage
2. resistance - within an established branch of the network
3. resistance - that calls for adding or deleting a branch of the network

## Increasing Voltage

First, we will conduct a variational analysis of this circuit to show what will happen if the applied voltage is increased from 60v to 120v.



	↑E <sub>a</sub>
I <sub>T</sub>	
R <sub>T</sub>	
P <sub>T</sub>	
I <sub>R1</sub>	
I <sub>R2</sub>	
I <sub>R3</sub>	
E <sub>R1</sub>	↑
E <sub>R2</sub>	↑
E <sub>R3</sub>	↑
R <sub>1</sub>	
R <sub>2</sub>	
R <sub>3</sub>	

In the top square, we indicate the variable, voltage, and that it is being increased (+).

It is immediately obvious that if E<sub>a</sub> is increased to 120v, then E<sub>R1</sub>, E<sub>R2</sub>, and E<sub>R3</sub> will increase to 120v because voltage is common in a parallel circuit. We indicate the voltage drop increase with arrows in the appropriate boxes.

#### What Happens to Branch Current

	↑E <sub>a</sub>
I <sub>T</sub>	
R <sub>T</sub>	
P <sub>T</sub>	
I <sub>R1</sub>	↑
I <sub>R2</sub>	↑
I <sub>R3</sub>	↑
E <sub>R1</sub>	↑
E <sub>R2</sub>	↑
E <sub>R3</sub>	↑
R <sub>1</sub>	
R <sub>2</sub>	
R <sub>3</sub>	

Now, if the applied voltage of this network is increased, then by Ohm's Law we know that branch current will increase in direct proportion to voltage.

Whereas current through each branch was 2 amps, when voltage was doubled, branch current was doubled.

$$I_{R1} = \frac{E_{R1}}{R_1}$$

$$I_{R1} = \frac{120v}{30\Omega} = 4 \text{ amps}$$

Therefore, we enter the appropriate arrows in the boxes to show increased branch current - I<sub>R1</sub>, I<sub>R2</sub>, and I<sub>R3</sub>.

Total Current

	$\uparrow E_a$
$I_T$	$\uparrow$
$R_T$	
$P_T$	
$I_{R1}$	$\uparrow$
$I_{R2}$	$\uparrow$
$I_{R3}$	$\uparrow$
$E_{R1}$	$\uparrow$
$E_{R2}$	$\uparrow$
$E_{R3}$	$\uparrow$
$R1$	
$R2$	
$R3$	

You know that if branch currents increase, total current also increases. The sum of the branch currents of a parallel network equal total current. We enter the increase arrow accordingly to show  $I_T$  has increased from 6 amps to 12 amps.

What Will Happen To Resistance

	$\uparrow E_a$
$I_T$	$\uparrow$
$R_T$	$\rightarrow$
$P_T$	
$I_{R1}$	$\uparrow$
$I_{R2}$	$\uparrow$
$I_{R3}$	$\uparrow$
$E_{R1}$	$\uparrow$
$E_{R2}$	$\uparrow$
$E_{R3}$	$\uparrow$
$R1$	$\rightarrow$
$R2$	$\rightarrow$
$R3$	$\rightarrow$

Since resistance is a physical factor, a change in voltage will not affect the value of the resistance.

Changing the applied voltage does not change the values of  $R1$ ,  $R2$ , or  $R3$ , and we fill in the appropriate arrows in the table ( $\rightarrow$ ).

As the values of the resistors remain the same, the equivalent resistance of this network remains the same. In the table we indicate that  $R_T$  does not change.

What Will Happen to Total Power

	$\uparrow E_a$
$I_T$	$\uparrow$
$R_T$	$\rightarrow$
$P_T$	$\uparrow$
$I_{R1}$	$\uparrow$
$I_{R2}$	$\uparrow$
$I_{R3}$	$\uparrow$
$E_{R1}$	$\uparrow$
$E_{R2}$	$\uparrow$
$E_{R3}$	$\uparrow$
$R1$	$\rightarrow$
$R2$	$\rightarrow$
$R3$	$\rightarrow$

When voltage is increased, total power will increase. This is evident when you recall the power formula,  $P = E \times I$ .

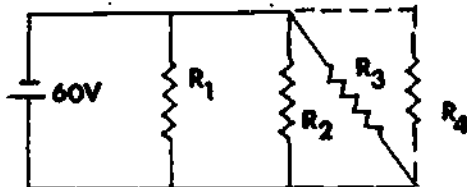
When voltage was increased to 120 volts, total current increased to 12 amps; therefore, total power must also increase.

Now we have completed a variational analysis of the circuit to show symbolically what would happen to every quantity if the applied voltage were increased.

Adding a Resistor

Consider now what will happen to our circuit if we vary resistance by adding another resistance.

If we add another resistor to this circuit, we are adding a fourth branch -- another path for current flow.





Effect on Current

	Add R4
$I_T$	↑
$R_T$	
$E_T$	
$P_T$	
$I_{R1}$	→
$I_{R2}$	→
$I_{R3}$	→
$E_{R1}$	
$E_{R2}$	
$E_{R3}$	
$R1$	
$R2$	
$R3$	

When we add R4 to the circuit, we provide another path for current. As current is additive in a parallel circuit, total current will increase.

Recall the rule that branch resistance determines branch current, and you can see that adding R4 will not affect current through the previously established branches.  $I_{R1}$ ,  $I_{R2}$ , and  $I_{R3}$  will remain the same.

What Happens to Voltage

	Add R4
$I_T$	↑
$R_T$	
$E_T$	→
$P_T$	
$I_{R1}$	→
$I_{R2}$	→
$I_{R3}$	→
$E_{R1}$	→
$E_{R2}$	→
$E_{R3}$	→
$R1$	
$R2$	
$R3$	

The applied voltage is determined by the source; therefore, adding R4 will not change total voltage. Because voltage is common,  $E_{R1}$ ,  $E_{R2}$ , and  $E_{R3}$  will not change.

The only change in voltage will be an additional voltage drop across R4.

What Happens to Resistance

	Add R4
$I_T$	↑
$R_T$	↓
$E_T$	→
$P_T$	
$I_{R1}$	→
$I_{R2}$	→
$I_{R3}$	→
$E_{R1}$	→
$E_{R2}$	→
$E_{R3}$	→
$R1$	→
$R2$	→
$R3$	→

Resistance in branches 1, 2, and 3 will not change because resistance is a physical property.

By the rules for parallel circuits, you know that if you add resistance to the network, the equivalent resistance decreases.  $R_T$ , then, will show a decrease arrow because we have added a fourth resistor to the network.

What Will Happen to Total Power

	Add R4
$I_T$	↑
$R_T$	↓
$E_T$	→
$P_T$	↑
$I_{R1}$	→
$I_{R2}$	→
$I_{R3}$	→
$E_{R1}$	→
$E_{R2}$	→
$E_{R3}$	→
$R1$	→
$R2$	→
$R3$	→

Total power is directly proportional to total current. When  $I_T$  increases,  $P_T$  must also increase, so we can complete our second variational analysis table by showing the increase arrow for  $P_T$ .

Varying Resistance in an Existing Branch

It is conceivable that you might want to increase or decrease the value of a resistor in an established branch of a parallel network. In such cases, you are not adding or removing a branch in the circuit, but you are changing the value of the resistance within a branch.

Assume that in the following circuit you increase the ohmic value of R<sub>1</sub> by replacing the 5-ohm resistor with a 10-ohm resistor.



### What Will Happen to Current

	↑R <sub>1</sub>
I <sub>T</sub>	↓
R <sub>T</sub>	
E <sub>T</sub>	
P <sub>T</sub>	↓
I <sub>R1</sub>	↓
I <sub>R2</sub>	→
E <sub>R1</sub>	
E <sub>R2</sub>	
R <sub>1</sub>	
R <sub>2</sub>	

When you increase resistance within a branch, by Ohm's Law you know that current within the branch will decrease.

Current in Branch 2 will not change.

Total current, then, being the sum of the branch currents, will decrease because  $I_{R1}$  decreased.

If  $I_T$  decreases, then total power also decreases.

### What Will Happen to Voltage

	↑R <sub>1</sub>
I <sub>T</sub>	↓
R <sub>T</sub>	
E <sub>T</sub>	→
P <sub>T</sub>	↓
I <sub>R1</sub>	↓
I <sub>R2</sub>	→
E <sub>R1</sub>	→
E <sub>R2</sub>	→
R <sub>1</sub>	
R <sub>2</sub>	

The applied voltage, of course, does not change when resistance changes. Because voltage is common in parallel networks,  $E_{R1}$  and  $E_{R2}$  will not change either.

What Will Happen to Resistance

	$\uparrow R_1$
$I_T$	$\downarrow$
$R_T$	$\uparrow$
$E_T$	$\rightarrow$
$P_T$	$\downarrow$
$I_{R1}$	$\downarrow$
$I_{R2}$	$\rightarrow$
$E_{R1}$	$\rightarrow$
$E_{R2}$	$\rightarrow$
$R_1$	$\uparrow$
$R_2$	$\rightarrow$

When voltage is constant, if total current decreases we know by Ohm's Law that  $R_T$  must have increased.

We physically increase resistance in branch 1, but branch 2 remains unchanged.

Practice

	$\downarrow R_{DS2}$
1. $I_T$	
$R_T$	
$E_T$	
$P_T$	
$R_{DS1}$	
$R_{DS3}$	
$E_{DS1}$	
$E_{DS2}$	
$E_{DS3}$	
$I_{DS1}$	
$I_{DS2}$	
$I_{DS3}$	

Recalling the rules for parallel circuits, conduct a variational analysis of this circuit if we replace  $DS_2$  with a 150w bulb. (Recall that a 150w bulb has less  $R$  than a 20w bulb.)



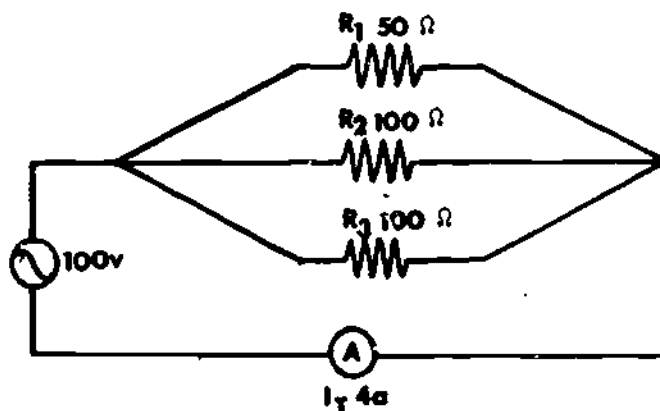
# Narrative

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2.

	1	2
	$E_a$	Add $R_4$
$I_T$		
$R_T$		
$E_T$		
$P_T$		
$I_{R1}$		
$I_{R2}$		
$I_{R3}$		
$E_{R1}$		
$E_{R2}$		
$E_{R3}$		
$R_1$		
$R_2$		
$R_3$		

Analyze this circuit, by completing column 1, to show what will happen if  $E_a$  is changed to 50v.



3.

Analyze the above circuit, by completing column 2, to show what will happen if we add another 50-ohm resistor in parallel to the network.

## Answers:

1.

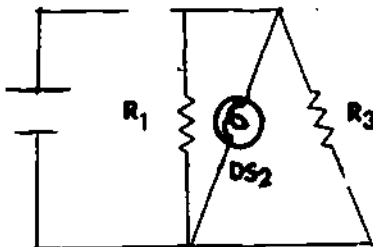
	$\downarrow R_{DS2}$
$I_T$	$\uparrow$
$R_T$	$\downarrow$
$E_T$	$\rightarrow$
$P_T$	$\uparrow$
$R_{DS1}$	$\rightarrow$
$R_{DS3}$	$\rightarrow$
$E_{DS1}$	$\rightarrow$
$E_{DS2}$	$\rightarrow$
$E_{DS3}$	$\rightarrow$
$I_{DS1}$	$\rightarrow$
$I_{DS2}$	$\uparrow$
$I_{DS3}$	$\rightarrow$

2 and 3.

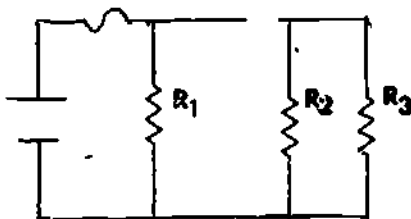
	$E_a$ ↓	Add R4
$I_T$	↓	↑
$R_T$	→	↓
$E_T$	↓	→
$P_T$	↓	↑
$I_{R1}$	↓	→
$I_{R2}$	↓	→
$I_{R3}$	↓	→
$E_{R1}$	↓	→
$E_{R2}$	↓	→
$E_{R3}$	↓	→
$R1$	→	→
$R2$	→	→
$R3$	→	→

### Opens In Main Lines - Affecting The Whole Network

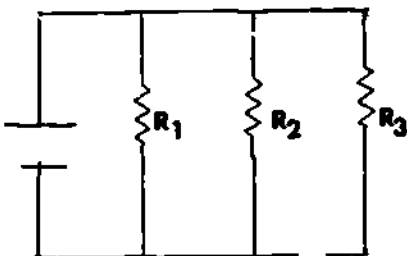
An open can also occur in the conductor which leads directly to, or from the source. How much of the network is affected depends on where the open occurs.



In this example, current does not have a complete path to follow, and it will stop entirely. The entire network is knocked out.



The open in this circuit will allow current flow in branch 1. It will stop current flow to both  $R_2$  and  $R_3$ , thus knocking them out of the network. Total current will be the current through  $R_1$ . Total current will decrease.



In this schematic the break is in the conductor on the line from the source, but it will affect only current to branch 3. The  $R_1$  and  $R_2$  branches will function normally.

NOW YOU MAY TAKE THE PROGRESS CHECK, OR YOU MAY STUDY ANY OF THE  
OTHER RESOURCES LISTED.

PROGRAMMED INSTRUCTION  
LESSON IIIVariational Analysis

TEST FRAMES ARE 8, 12, 20, AND 25. AS BEFORE, GO FIRST TO TEST FRAME 8 AND SEE IF YOU CAN ANSWER ALL THE QUESTIONS THERE. FOLLOW THE DIRECTIONS GIVEN AFTER THE TEST FRAME.

---

1. Before going into variational analysis, you must understand the nature of the values you are dealing with. Recall that voltage is a potential difference that causes current flow. Voltage is said to be an independent variable in that it is controlled from outside the circuit (changing batteries, etc.).

For example, an increase in source voltage would cause an increase in circuit current, but an increase in circuit current would not cause an increase in applied voltage.

A decrease in applied voltage would cause  $I_T$  to:

- ☐ a. increase.  
☐ b. decrease.  
☐ c. remain the same.
- 

(b) decrease

2. The second circuit value, current, is known as a dependent variable because it is dependent upon applied voltage and circuit resistance.

If applied voltage were doubled and circuit resistance were halved,  $I_T$  would;

- ☐ a. remain the same.  
☐ b. double.  
☐ c. triple.  
☐ d. quadruple.
- 

(d) quadruple



3. The third circuit value is resistance. As you will recall, resistance is a physical factor. This means that if resistance is to change, something must actually be done to the resistor or circuit (variable resistor, replacement of resistor, etc.).

If circuit current doubles, resistance will:

- ☐ a. increase.
- ☐ b. decrease.
- ☐ c. remain the same.

-----  
\_\_\_\_\_  
(c) remain the same  
\_\_\_\_\_

4. Ohm's Law states that current is directly affected by \_\_\_\_\_ and inversely by resistance. Current is the dependent variable and is affected by both resistance and voltage. On the other hand, current does not determine what applied voltage and circuit resistance will be. They are independent variables.

-----  
\_\_\_\_\_  
(voltage)  
\_\_\_\_\_

5. Recall that in a parallel circuit  $R_T$  ( $R_T$ ) decreases each time another current path (branch) is added.

Using arrows to show increase ( $\uparrow$ ), decrease ( $\downarrow$ ), and remain the same ( $\rightarrow$ ), indicate what will happen to each circuit value when SW1 is closed.

a.  $E_a$  \_\_\_\_\_

b.  $R_T$  \_\_\_\_\_

c.  $I_T$  \_\_\_\_\_

d.  $R1$  \_\_\_\_\_

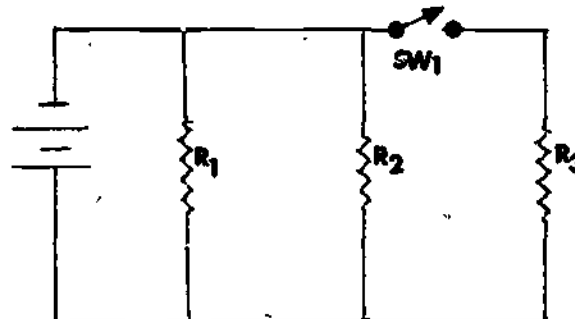
e.  $R2$  \_\_\_\_\_

f.  $R3$  \_\_\_\_\_

g.  $I_{R1}$  \_\_\_\_\_

h.  $I_{R2}$  \_\_\_\_\_

i.  $I_{R3}$  \_\_\_\_\_



(a.  $E_a$   $\rightarrow$ )

b.  $R_T$   $\downarrow$

c.  $I_T$   $\uparrow$

d.  $R1$   $\rightarrow$

e.  $R2$   $\rightarrow$

f.  $R3$   $\rightarrow$

g.  $I_{R1}$   $\rightarrow$

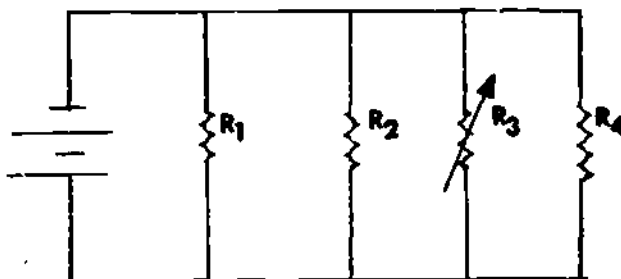
h.  $I_{R2}$   $\rightarrow$

i.  $I_{R3}$   $\uparrow$ )

6. Any variation within an existing branch will cause a corresponding change in  $R_{eq}$  and  $I_T$ . For example, if branch 1 resistance were increased, this would cause an increase in  $R_T$  and a decrease in  $I_T$ .

Using arrows, indicate the changes which would occur if the value of  $R_3$  were decreased.

- a.  $I_T$  \_\_\_\_\_  
 b.  $R_T$  \_\_\_\_\_  
 c.  $I_{R1}$  \_\_\_\_\_  
 d.  $I_{R2}$  \_\_\_\_\_  
 e.  $I_{R3}$  \_\_\_\_\_  
 f.  $I_{R4}$  \_\_\_\_\_



- a.  $I_T$   $\uparrow$   
 b.  $R_T$   $\downarrow$   
 c.  $I_{R1}$   $\rightarrow$   
 d.  $I_{R2}$   $\rightarrow$   
 e.  $I_{R3}$   $\uparrow$   
 f.  $I_{R4}$   $\rightarrow$

7. A change in applied voltage will cause a direct change in all values of current, voltage, and power within the circuit.

Using arrows, indicate the changes which would take place if source voltage were doubled.

a.  $I_T$  \_\_\_\_\_

b.  $R_{eq}$  \_\_\_\_\_

c.  $R1$  \_\_\_\_\_

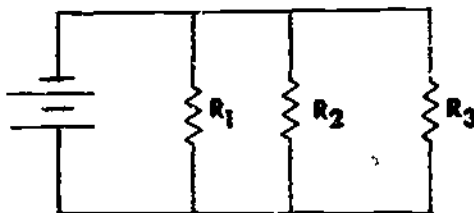
d.  $R2$  \_\_\_\_\_

e.  $R3$  \_\_\_\_\_

f.  $I_{R1}$  \_\_\_\_\_

g.  $I_{R2}$  \_\_\_\_\_

h.  $I_{R3}$  \_\_\_\_\_




---

a.  $I_T$  ↑

b.  $R_{eq}$  +

c.  $R1$  +

d.  $R2$  +

e.  $R3$  +

f.  $I_{R1}$  ↑

g.  $I_{R2}$  ↑

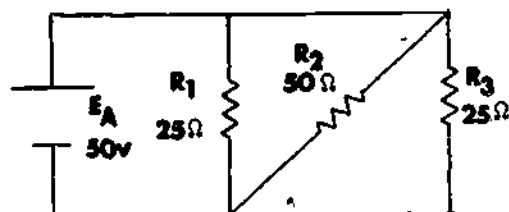
h.  $I_{R3}$  ↑

---

P.1.

Six-III

8. Place arrows to show increase (+), decrease (-), or same (→) in each box of the variational analysis table in accordance with these questions.



- What will happen to the other quantities if total  $E$  is increased to 100V?
- What will happen to the other quantities if a 50-ohm resistor is added in parallel?
- What will happen to the other quantities if  $R_1$  is replaced with a 20-ohm resistor?

a.      b.      c.

	$E_a$	Add $R_4$	$R_1$
$I_T$			
$E_T$			
$R_T$			
$P_T$			
$I_{R1}$			
$I_{R2}$			
$I_{R3}$			
$R_1$			
$R_2$			
$R_3$			
$E_{R1}$			
$E_{R2}$			
$E_{R3}$			

(THIS IS A TEST FRAME. COMPARE YOUR ANSWERS WITH THE CORRECT ANSWERS GIVEN AT THE TOP OF THE NEXT PAGE.)

## ANSWERS - TEST FRAME 8

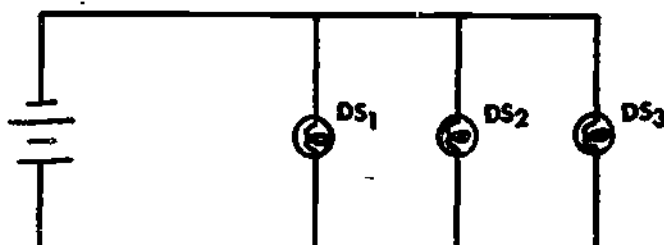
a.      b.      c.

	$E_a \uparrow$	Add R4	$\downarrow R1$
$I_T$	$\uparrow$	$\uparrow$	$\uparrow$
$E_T$	$\uparrow$	$\rightarrow$	$\rightarrow$
$R_T$	$\rightarrow$	$\downarrow$	$\downarrow$
$P_T$	$\uparrow$	$\uparrow$	$\uparrow$
$I_{R1}$	$\uparrow$	$\rightarrow$	$\uparrow$
$I_{R2}$	$\uparrow$	$\rightarrow$	$\rightarrow$
$I_{R3}$	$\uparrow$	$\rightarrow$	$\rightarrow$
$R1$	$\rightarrow$	$\rightarrow$	$\downarrow$
$R2$	$\rightarrow$	$\rightarrow$	$\rightarrow$
$R3$	$\rightarrow$	$\rightarrow$	$\rightarrow$
$E_{R1}$	$\uparrow$	$\rightarrow$	$\rightarrow$
$E_{R2}$	$\uparrow$	$\rightarrow$	$\rightarrow$
$E_{R3}$	$\uparrow$	$\rightarrow$	$\rightarrow$

IF ALL YOUR ANSWERS MATCH THE CORRECT ANSWERS, YOU MAY GO ON TO TEST FRAME 12. OTHERWISE, GO BACK TO FRAME 1 AND TAKE THE PROGRAMMED SEQUENCE BEFORE TAKING TEST FRAME 8 AGAIN.

9. Parallel circuits have one distinct advantage over series circuits in that an open in one branch will not affect the operation of the other branches and a variation of resistance (within reasonable limits) will not affect the other branches.

If DS2 burns out, DS1 and DS3 will:



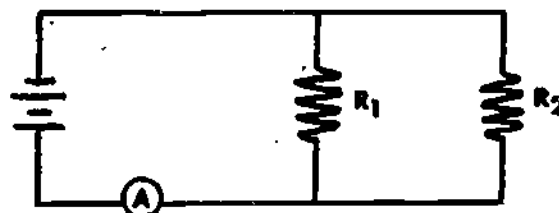
- ☐ a. become dimmer.  
☐ b. become brighter.  
☐ c. not change.

---

(c) not change

---

10. Check the arrow that indicates what will happen to the ammeter reading if R1 opens.



- ☐ a. +  
☐ b. +  
☐ c. +

---

(a) +

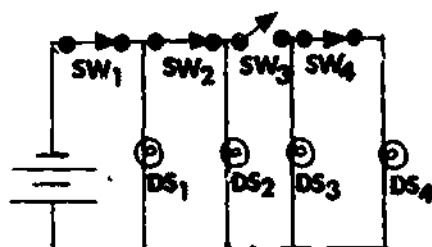
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P.1.

Six-III

11. Should an open occur within a branch of a parallel circuit, only that branch would be affected; should the open isolate more than one branch, only the branches beyond the open will be affected. All others will function normally.

Indicate what would happen to each light bulb if SW3 were closed.



1. DS1  
2. DS2  
3. DS3  
4. DS4

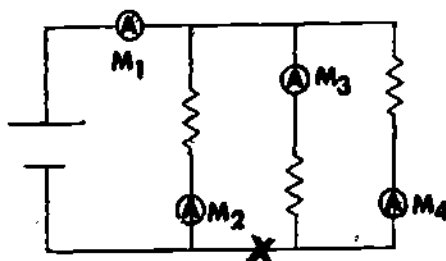
- a. brighten  
b. dim  
c. go out  
d. remain the same

(1. d; 2. d; 3. a; 4. a)

12. Match the lettered choice in column B to the meter symbols in column A to indicate what will happen to each meter in this circuit if an open occurs at the X.

A

1. M1  
2. M2  
3. M3  
4. M4



B

- a. +  
b. +  
c. +  
d. goes to zero

(THIS IS A TEST FRAME. COMPARE YOUR ANSWERS WITH THE CORRECT ANSWERS GIVEN AT THE TOP OF THE NEXT PAGE.)



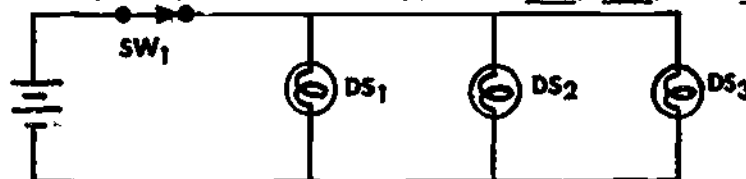
## ANSWERS - TEST FRAME 12

1. c
2. a
3. d
4. d

IF ALL YOUR ANSWERS MATCH THE CORRECT ANSWERS, YOU MAY GO ON TO TEST FRAME 20. OTHERWISE, GO BACK TO FRAME 9 AND TAKE THE PROGRAMMED SEQUENCE BEFORE TAKING TEST FRAME 12 AGAIN.

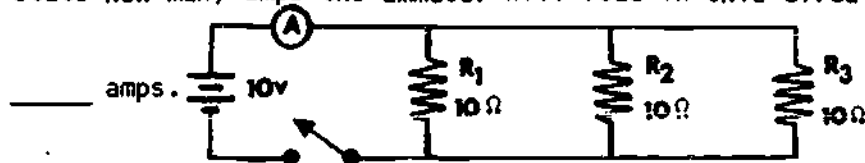
13. Although an open in a branch will decrease total current, it will not stop all circuit action. To completely de-energize a circuit, the open must occur at an electrically common point (point through which all circuit current must pass).

If SW<sub>1</sub> were opened, what would happen to DS<sub>1</sub>, DS<sub>2</sub>, and DS<sub>3</sub>.



(go out)

14. State how many amps the ammeter will read in this circuit.



(0)

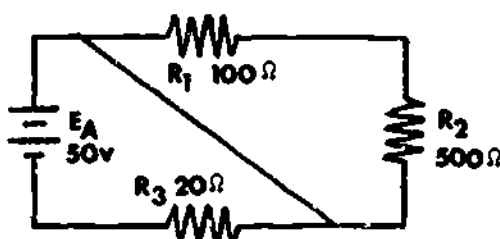
15. An open in a parallel circuit will not necessarily have the same effect as it would in a series circuit. To completely stop all circuit action in parallel, the open must occur at an electrically common point, whereas in a \_\_\_\_\_ circuit, an open anywhere would de-energize the entire circuit.

(series)

16. A short circuit is an accidental low-resistance path for current flow. Regardless of the type of circuit, a short will have the same effect, an increase in total current.

What is  $I_T$ ?

- a. 83 ma  
b. 100 ma  
c. 300 ma  
d. 2500 ma



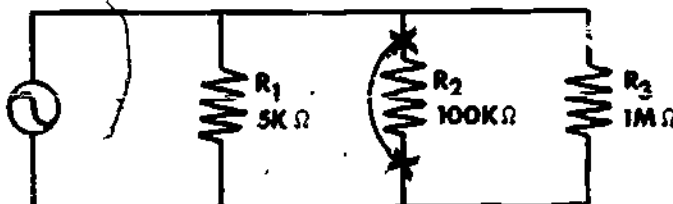
(d) 2500 ma

17. As you will recall,  $R_T$  in a parallel circuit is always \_\_\_\_\_ than the least branch resistance. If a direct short is placed across a parallel circuit at any point, the total resistance is effectively reduced to 0. In the case of a partial short,  $R_T$  would be something less than normal.

(smaller, or less)

18. Solve for  $R_T$ .

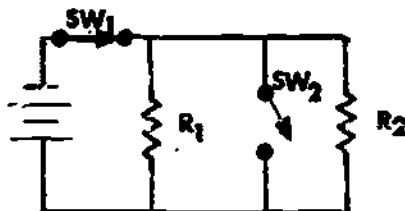
$R_T$  \_\_\_\_\_



(0)

19. If a circuit is shorted, it will pass an abnormally large current. Due to the extremely small resistance of the short (usually considered 0), all of the current will flow through the short, and none will flow through the load.

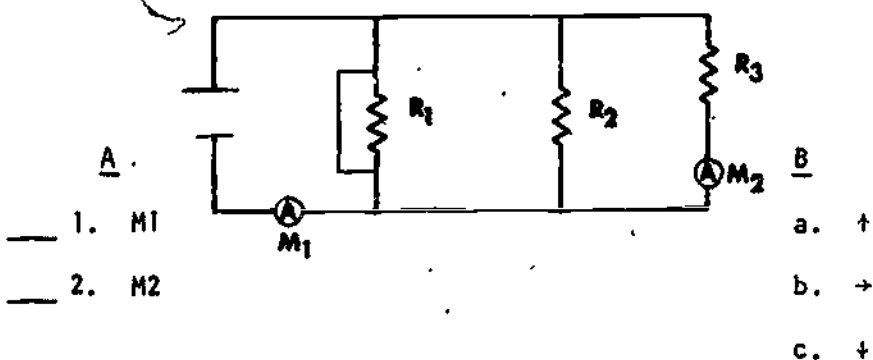
Indicate how each value will be affected if SW2 is closed.



- |             |                  |
|-------------|------------------|
| 1. $I_T$    | a. $\uparrow$    |
| 2. $I_{R1}$ | b. $\rightarrow$ |
| 3. $I_{R2}$ | c. $\uparrow$    |

(1. a; 2. c; 3. c)

20. Match the letter choice in column B to the meter symbols in column A to indicate what will happen to each meter in this circuit if the short occurs as indicated.



(THIS IS A TEST FRAME. COMPARE YOUR ANSWERS WITH THE CORRECT ANSWERS GIVEN AT THE TOP OF THE NEXT PAGE.)

---

ANSWERS - TEST FRAME 20

---

1. a

2. c

---

IF ALL YOUR ANSWERS MATCH THE CORRECT ANSWERS, YOU MAY GO ON TO TEST FRAME 25. OTHERWISE, GO BACK TO FRAME 13 AND TAKE THE PROGRAMMED SEQUENCE BEFORE TAKING TEST FRAME 20 AGAIN.

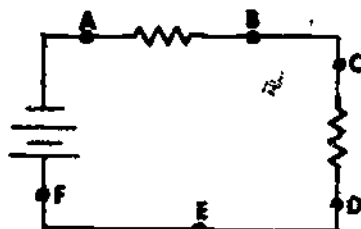
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21. Recall that a fuse is placed in a circuit to protect against excessive current. To do this, the fuse must be placed in series with the source.

At which point could the fuse be placed?

☐ a. A☐ b. B☐ c. C☐ d. D☐ e. any of the above

---



---

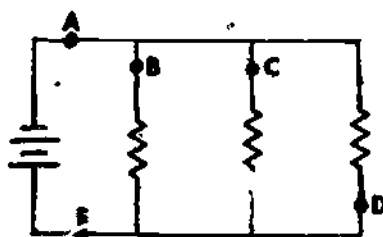
(e) any of the above

---

22. In a series circuit, the fuse can be placed at any point and still be in series with the source. To protect a parallel circuit, you must ensure that the fuse is placed at an electrically common point so that all the circuit current passes through it.

Where could the fuse be placed to protect the entire circuit?

- ☐ a. A  
☐ b. B  
☐ c. C  
☐ d. D  
☐ e. E

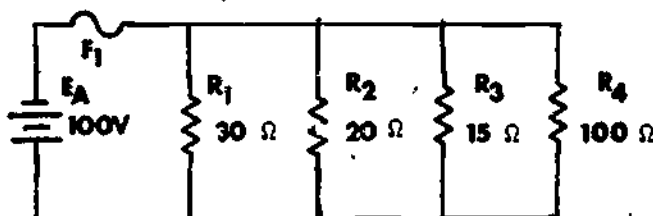


(a. A; e. E)

23. Recall that fuses are rated in amps; if the rated value is exceeded, the filament burns out, and the circuit is de-energized.

The fuse is rated at 15 amps. Will this circuit remain operative?

- ☐ a. yes  
☐ b. no



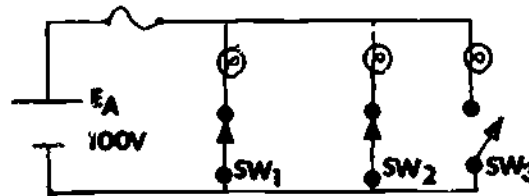
(b) no

24. One of the most common reasons for a fuse to blow in a parallel circuit is excessive current caused by adding too many load devices.

Adding additional loads in parallel causes  $I_T$  to increase/decrease.

(Increase)

25. Check the probable explanations of why the fuse would blow when SW3 is closed.



- ☐ a. The fuse must be defective.
- ☐ b. Current will exceed the fuse rating.
- ☐ c. There are too many loads.
- ☐ d. SW3 must be defective.
- 

(THIS IS A TEST FRAME. COMPARE YOUR ANSWERS WITH THE CORRECT ANSWERS AT THE TOP OF THE NEXT PAGE.)

---

**ANSWERS - TEST FRAME 25**

- b. Current will exceed the fuse rating.
  - c. There are too many loads.
- 
- 

IF ANY OF YOUR ANSWERS ARE INCORRECT, GO BACK TO FRAME 21 AND TAKE THE PROGRAMMED SEQUENCE.

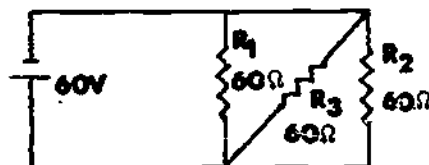
IF YOUR ANSWERS ARE CORRECT, YOU MAY TAKE THE PROGRESS CHECK, OR YOU MAY STUDY ANY OF THE OTHER RESOURCES LISTED. IF YOU TAKE THE PROGRESS CHECK AND ANSWER ALL THE QUESTIONS CORRECTLY, GO ON TO THE NEXT LESSON. IF NOT, STUDY ANY METHOD OF INSTRUCTION YOU WISH UNTIL YOU CAN ANSWER ALL THE QUESTIONS CORRECTLY.

SUMMARY  
LESSON III

Variational Analysis

A quick way to improve your understanding of how circuit quantities interact is to use variational analysis. In variational analysis, one value in a circuit is caused to change and the effect of this change on all other circuit quantities is examined. A table is made up listing all measurable values in a circuit, and arrows are used to show what changes take place. An arrow pointing upward indicates increase (+); an arrow downward, decrease (-); and a horizontal arrow, no change ( $\rightarrow$ ). Variational analysis usually starts with an assumed change in either voltage or resistance, the quantities we can physically change in a circuit.

Here is an example of changing the applied voltage in a circuit from 60v to 120v.



First, show in the top square the value which has changed and whether it increases or decreases; then mark in arrows which show how the remaining values are affected. You need not work out values unless you are uncertain of the answer; you should be able to fill in the blanks from your knowledge of Ohm's Law and circuit rules.

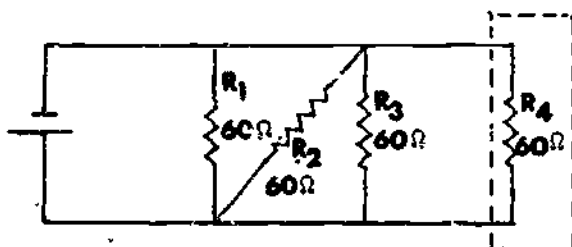
	$E_a$ ↑
$I_T$	↑
$R_T$	$\rightarrow$
$P_T$	↑
$I_{R1}$	↑
$I_{R2}$	↑
$I_{R3}$	↑
$E_{R1}$	↑
$E_{R2}$	↑
$E_{R3}$	↑
$R1$	$\rightarrow$
$R2$	$\rightarrow$
$R3$	$\rightarrow$



## Summary

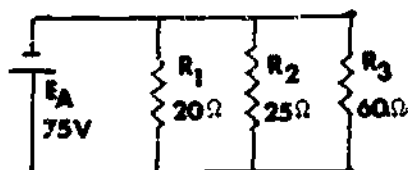
Six-III

Another change could be the addition of another branch to the circuit; here is an analysis of such a change:



	Add R4
$I_T$	↑
$R_T$	↓
$P_T$	↑
$I_{R1}$	→
$I_{R2}$	→
$I_{R3}$	→
$E_{R1}$	→
$E_{R2}$	→
$E_{R3}$	→
$R1$	→
$R2$	→
$R3$	→

A third change we could make is to vary one of the resistance values in an existing circuit. Suppose that the resistance of  $R3$  in the circuit below is changed from 50 ohms to 200 ohms. For this example, you fill in the boxes.



	R3
$I_T$	
$R_T$	
$P_T$	
$I_{R1}$	
$I_{R2}$	
$I_{R3}$	
$E_{R1}$	
$E_{R2}$	
$E_{R3}$	
$R1$	
$R2$	
$R3$	

Answer:

	▲R3
I <sub>T</sub>	▼
R <sub>T</sub>	▲
P <sub>T</sub>	▼
I <sub>R1</sub>	→
I <sub>R2</sub>	→
I <sub>R3</sub>	▼
E <sub>R1</sub>	→
E <sub>R2</sub>	→
E <sub>R3</sub>	→
R <sub>1</sub>	→
R <sub>2</sub>	→
R <sub>3</sub>	▲

AT THIS POINT YOU MAY TAKE THE LESSON PROGRESS CHECK, OR YOU MAY STUDY THE LESSON NARRATIVE OR THE PROGRAMMED INSTRUCTION OR BOTH. IF YOU TAKE THE PROGRESS CHECK AND ANSWER ALL OF THE QUESTIONS CORRECTLY, GO TO THE NEXT LESSON. IF NOT, SELECT ANOTHER METHOD OF INSTRUCTION UNTIL YOU CAN ANSWER ALL THE QUESTIONS CORRECTLY.



BASIC ELECTRICITY AND ELECTRONICS  
INDIVIDUALIZED LEARNING SYSTEM



MODULE SIX  
LESSON IV

Troubleshooting Parallel Circuits

Study Booklet

OVERVIEW  
LESSON IV

Troubleshooting Parallel Circuits

In this lesson, you will study and learn about the following:

- shorts
- opens
- practical experiments in troubleshooting

Each of the above topics will be discussed in the order listed. As you proceed through this lesson, observe and follow directions carefully.

BEFORE YOU START THIS LESSON, PREVIEW THE LIST OF STUDY RESOURCES ON THE NEXT PAGE.

LIST OF STUDY RESOURCES  
LESSON IV

Troubleshooting Parallel Circuits

To learn the material in this lesson, you have the option of choosing, according to your experience and preferences, any or all of the following:

STUDY BOOKLET:

Lesson Narrative

Lesson Summary

ENRICHMENT MATERIAL:

NAVPERS 93400a-1a "Basic Electricity, Direct Current."

Fundamentals of Electronics. Bureau of Naval Personnel.  
Washington, D.C.: U.S. Government Printing Office, 1965.

YOU MAY NOW STUDY ANY OR ALL OF THE RESOURCES LISTED ABOVE. YOU MAY  
TAKE THE PROGRESS CHECK AT ANY TIME.

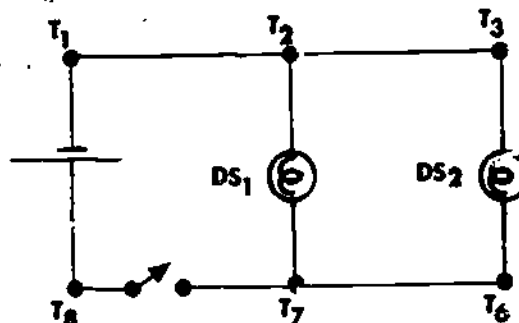
# NARRATIVE LESSON IV

## Troubleshooting Parallel Circuits

Do all of the following experiments as you go through this narrative.

### Experiment #1 - Voltage

- Using Practice Board 0-1 and one dry cell, construct the following circuit:

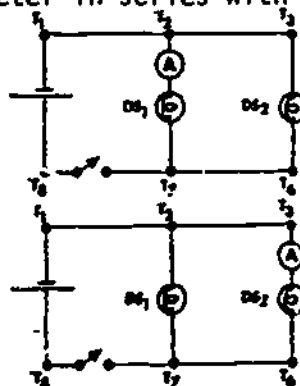


- Set up multimeter as voltmeter.
- Close switch.
- Measure voltage across the terminals of the source.  
 $E_a = \underline{\hspace{2cm}}$
- Measure voltage across the branch with DS1, between T2 and T7.  
 $E_a = \underline{\hspace{2cm}}$
- Measure voltage across the branch with DS2, between T3 and T6.  
 $E_a = \underline{\hspace{2cm}}$

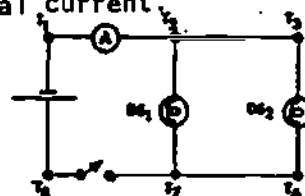
You have observed that the voltage drop across each parallel branch is, for all practical purposes, equal to the applied voltage. In a parallel circuit, voltage is common to all branches.

### Experiment #2 - Current

- Using Practice Board 0-1 set up as for experiment 1, connect multimeter as ammeter in series with DS1.
- Close switch.
- Record current in branch 1.
- Open switch.
- Connect ammeter in series with DS2.
- Close switch.



7. Record current in branch 2.
8. Open switch.
9. Compute total current by adding branch currents.
10. Now prove your answer  $I_T =$  in No. 9 is true by connecting ammeter between T1 and T2 to read total current.
11. Close switch.
12. Record ammeter reading.
13. Open switch.



This experiment proves visually to you that the sum of the branch currents equals total current. You can also see this by doing another experiment.

### Experiment #3

1. With Practice Board 0-1 set as in experiment #2, connect ammeter to measure total current.
2. Close switch.
3. Unscrew bulb in branch 2. Does bulb in branch 1 go out? Does bulb in branch 1 get dimmer or brighter?

You have seen that an open branch in a parallel circuit does not affect another branch. Current through each branch is determined by the branch resistance and the applied voltage.

4. Now, tighten bulb in branch 2. Read total current with both bulbs drawing current.

5. Loosen bulb in branch 1 and read total current.

Total current has decreased, because one branch current has been subtracted from it.

6. Tighten bulb 1, loosen bulb 2 and read total current.

7. Open switch.

Experiments have shown you that in parallel circuits:

1. Voltage is common.
2. Branch current is determined by branch resistance and applied voltage.



3. Total current is equal to the <sup>4</sup>sum of the individual branch currents.

### Troubleshooting

You recall from our study of series circuits that there are two problems that can cause a malfunction in circuits. These are short circuits and open circuits.

### Shorts

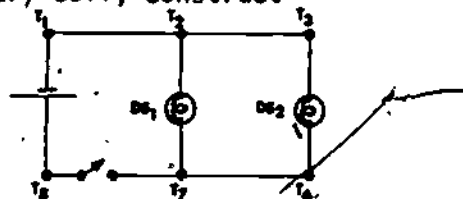
When a short occurs in a parallel circuit, it places a direct short across the power lines -- the wire leading from the source and the wire leading back to the source.

The exception to this is when part of a component is shorted. Then we have a partial short.

### Experiment #4

Let's create a direct short!

- Using Practice Board 0-1 and one dry cell, construct the following circuit:



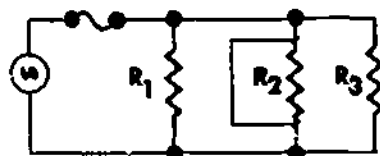
- Close switch.
- Cause a short across the lamp in branch 1 by placing a wire between terminals T2 and T7.
- What happens to the light in branch 1? \_\_\_\_\_  
To the light in branch 2? \_\_\_\_\_
- What path must current be taking? \_\_\_\_\_
- Remove the wire causing the short.
- Open switch.

You observed that when a short was caused across branch 1, all circuit current followed the path through the short. We say that current follows the path of least resistance.

When there is no circuit resistance, current will be very high, because nothing is limiting the amount of current flow (except internal source resistance and the resistance of the wire).

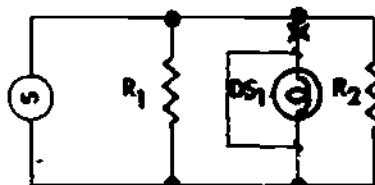
## Narrative

Six-IV

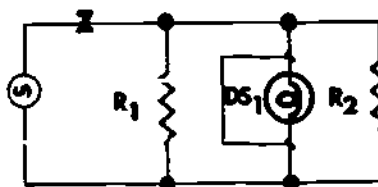


Notice there is a short across  $R_2$  in this schematic. Current will take the path of least resistance -- all circuit current will go through the short. Then, because current will increase tremendously, it will exceed the fuse rating. The fuse will blow, and current will stop.

If there were no fuse, the wires would become overheated and catch fire, thus a short could cause an open.



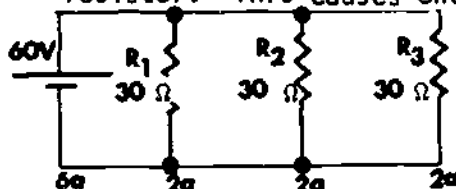
If the conductor opened at point  $X$ , then  $R_1$  and  $R_3$  could resume normal operation, with branch resistance controlling branch current.



If, however, the wire overheated and opened at point  $Z$ , all current in the network would stop. This is a main-line open which we will discuss shortly.

## Branch Opens

Branch one in the following parallel network has a burned out resistor. This causes one branch of the network to be open.



This open does not affect branch 2 or 3. It will, however, cause total current to decrease to  $4a$ , because there is no current through  $R_1$ .

Total resistance was  $10\Omega$ , but with  $R_1$  out of the picture, total resistance increases to  $15\Omega$ .

If an open occurred as shown in the schematic above:

$I_T$  would (increase/decrease).

$R_T$  would (increase/decrease).

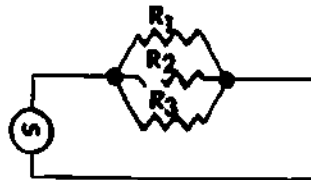
$P_T$  would (increase/decrease).

$I_T$  would decrease;  $R_T$  would increase;  $P_T$  would decrease.

Recalling all you have learned about shorts and opens in parallel networks, practice these problems, then check your answers against the correct answers. Be sure to study the schematics carefully.

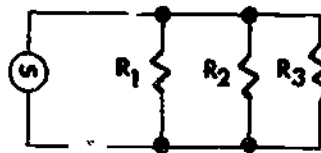
1. Which branch or branches will be knocked out of the circuit by the problem observable in the schematic?

(a).



\_\_\_\_\_

(b).



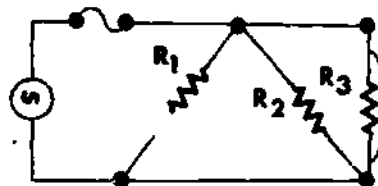
\_\_\_\_\_

2. Compare these quantities to a normal circuit condition. Will they increase, decrease, or remain the same?

$I_T$  \_\_\_\_\_

$R_T$  \_\_\_\_\_

$E_A$  \_\_\_\_\_



Check answers on next page.

## ANSWERS:

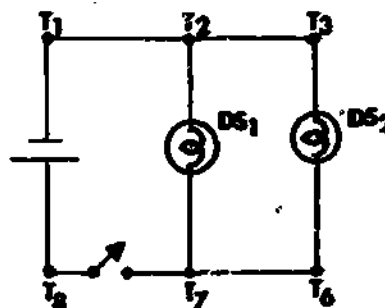
1. (a) R2  
(b) R1, R2 and R3
2. No doubt you caught the open (R1) in the circuit and you also noticed that the third leg of the network has a shorted resistor in it. Therefore, it is a direct short. All current will flow through the short, bypassing the other two branches. Therefore:

 $I_T$  increase $R_T$  decrease $E_a$  same

When current exceeds fuse rating -- fuse will blow and then everything will stop.

Experiment #5Locating Shorts With a Meter

1. Construct a parallel circuit on Practice Board 0-1 according to the schematic.
2. Leave switch open.
3. Connect a wire across DS2 between T3 and T6.



This creates a short in branch 2 of the network. Assuming we do not know where the short is, let's hunt for it. We will do this by systematically checking each branch of the circuit.

4. Take a visual check looking for signs of overheating, such as charred parts or smoke damage. If the visual check does not locate the problem, then set up the ohmmeter.
5. Because a parallel circuit has more than one path for current flow, it is difficult to locate a short unless

we check each branch systematically. Operating a circuit with a short in it may cause considerable damage to good components, so most troubleshooting should be done with an ohmmeter. Let's begin by making sure the circuit has no voltage across the branches, then connecting the ohmmeter across the loads. For this circuit, clip the test leads to points T2 and T7.

What is the ohmmeter reading? \_\_\_\_\_

(0Ω)

6. Place probes across T2 and T7. You measure 0 but you know that there should be some resistance in the bulb.
7. Disconnect the wire from DS1 to T2.
8. Measure across T2 and T7 again. You still get a 0 reading indicating the circuit still is shorted; therefore, the trouble does not occur in this branch.
9. Reconnect DS1, disconnect DS2 and the wire shorting it.
10. Measure across DS1. The meter reads some resistance, indicating that the short has been isolated. You have located the short as being in branch 2.
11. Now the problem can be corrected and the circuit restored to normal.

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AT THIS POINT, YOU MAY TAKE THE PROGRESS CHECK, OR YOU MAY STUDY ANY OF THE OTHER RESOURCES LISTED. IF YOU TAKE THE PROGRESS CHECK AND ANSWER ALL OF THE QUESTIONS CORRECTLY, YOU HAVE MASTERED THE MATERIAL AND ARE READY TO TAKE THE MODULE TEST. SEE YOUR CLASSROOM SUPERVISOR.

IF YOU DECIDE NOT TO TAKE THE PROGRESS CHECK AT THIS TIME, OR IF YOU MISSED ONE OR MORE QUESTIONS, STUDY ANY METHOD OF INSTRUCTION YOU WISH UNTIL YOU HAVE ANSWERED ALL THE PROGRESS CHECK QUESTIONS CORRECTLY. THEN SEE YOUR CLASSROOM SUPERVISOR AND ASK TO TAKE THE MODULE TEST.

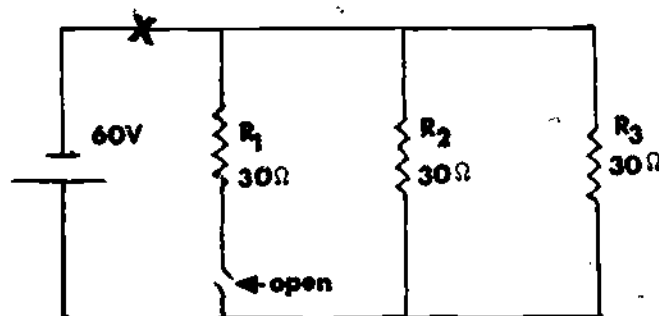
SUMMARY  
LESSON IV

Troubleshooting Parallel Circuits

Short circuits and open circuits are the sources of trouble in parallel circuits just as they were in series circuits. A direct short in a parallel circuit will bypass the current around all the branches, for current always follows the path of least resistance. The direct short will cause very high current flow which will cause the internal resistance of the source to drop all of the source voltage. If the circuit is not protected by fuses, the source or wiring will soon be damaged.

Short circuits in parallel circuits are usually located with an ohmmeter, if fire and smoke do not show the source of the trouble first. The procedure used is to connect the ohmmeter across the de-energized circuit, then disconnect the branches, one at a time, until the short (0) reading disappears. The defect in that branch can then be corrected and the circuit restored to operation.

Open circuits may affect all or any part of a parallel circuit; that is, one branch may open or the entire circuit may be opened. In the diagram below, the open in branch 1 affects only three factors in the circuit,  $I_1$ ,  $I_T$ , and  $R_T$ . If the open occurs at the point marked X, however,  $I_T$  drops to 0 and the entire circuit is dead.



Open circuits may be found using an ohmmeter and disconnecting branches again -- this time you must watch for a branch which does not cause a change in the resistance reading.

The narrative for this lesson contains a variety of experiments which you should perform if you have not previously worked with circuits.

AT THIS POINT, YOU MAY TAKE THE LESSON PROGRESS CHECK, OR YOU MAY STUDY THE LESSON NARRATIVE. IF YOU TAKE THE PROGRESS CHECK AND ANSWER ALL OF THE QUESTIONS CORRECTLY, GO TO THE NEXT LESSON. IF NOT, STUDY ANOTHER METHOD OF INSTRUCTION UNTIL YOU CAN ANSWER ALL THE QUESTIONS CORRECTLY.